

# Optimal (Un)Conventional Monetary Policy

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# Motivation

- ▶ **Central Banking** with **many policy instruments**:
  - ▶ Interest rate on excess reserves
  - ▶ Interest rate on required reserves
  - ▶ Reserve requirements
  - ▶ Balance sheet management: purchases/sales of long-term gov. bonds in exchange for reserves

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  - ▶ Reserve requirements
  - ▶ Balance sheet management: purchases/sales of long-term gov. bonds in exchange for reserves
- ▶ What role does each instrument play? How do they interact?
- ▶ What is the welfare-maximizing policy mix?

# Balance Sheets

Central Bank	
A	L
<i>L</i> -Bonds	Reserves

Intermediaries	
A	L
<i>L</i> -Bonds	Deposits
Reserves	
Outside Equity	
	Net worth

Households	
A	L
Deposits	Outside Equity
<i>L</i> -Bonds	Net worth
Capital $k$	

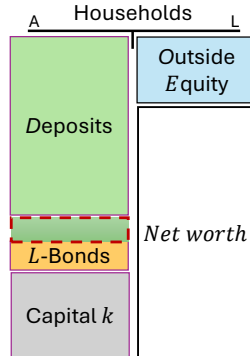
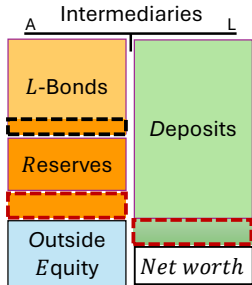
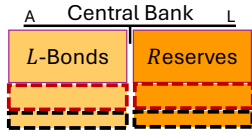
# Balance Sheet Management: L-Bond purchases from Households

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# Balance Sheet Management: L-Bond purchases from HH & Banks



# Overview

- ▶ Macro model with financial sector, aggregate & idiosyncratic risk, sticky prices  
Brunnermeier & Sannikov (2016), Li & Merkel (2025), Merkel (2020)
- ▶ No constraint-relaxing role of QE, endogenous duration risk distribution  
Gertler & Karadi (2011), Karadi & Nakov (2021), Eren, Jackson & Lombardo (2024)

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  - ▶ Balance sheet policy mediates the effects of bond price fluctuations:

$$\frac{P_t^L L_t}{\mathcal{R}_t + P_t^L L_t} \frac{\partial \log P_t^L}{\partial \log x_t}$$

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- ▶ Interest rate policy alone can implement the efficient path of *aggregates*
- ▶ Adding *distributional* efficiency requires active balance sheet management

# NK Framework with Financial Sector — Risk Focus

## ► Households/Entrepreneurs:

- Hold capital, utilize it in production ( $v_t$ ) and invest ( $l_t$ )
- Capital accumulation is subject to uninsurable idiosyncratic risk:

$$\frac{dk_t}{k_t} = \left( \frac{1}{\phi} \log(1 + \phi l_t) - \delta \right) dt + \tilde{\sigma}_t d\tilde{Z}_t \quad d\tilde{\sigma}_t^2 = -b_s(\tilde{\sigma}_t^2 - \tilde{\sigma}_{ss}^2)dt + \sigma \tilde{\sigma}_t^2 dZ_t$$

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  - More deposits  $\implies$  lower velocity  $v_t$  and lower transaction cost  $t(v_t)$
- Issue risky claims on capital to intermediaries, passing on fraction  $\chi_t$  of risk

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## ► Sticky prices à la Rotemberg

## Constrained Efficiency

- ▶ Suppose the government raises taxes over time (flow/ $dt$  taxes) and in response to aggregate shocks (loading on  $dZ_t$ ), but not to idios. shocks (not on  $d\tilde{Z}_t$ )



## Constrained Efficiency

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- ▶ Behaves as a planner that can freely set:
  - ▶ Capital utilization rate  $v_t$
  - ▶ Capital investment rate  $\iota_t$
  - ▶ Distribution of wealth/consumption across sectors  $\eta_t = N_t^I/N_t$ ,
  - ▶ Distribution of wealth across assets  $\vartheta_t = \mathcal{B}_t/(\mathcal{P}_t N_t) = (\mathcal{R}_t + P_t^L L_t)/(\mathcal{P}_t N_t)$
  - ▶ Distribution of idiosyncratic risk exposure  $\chi_t$

# Constrained Efficiency

► Planner's objective:

$$\begin{aligned} \max_{\{\iota_t, v_t, \vartheta_t, \eta_t, \chi_t\}_{t=0}^{\infty}} & \lambda \mathbb{E} \int_0^{\infty} e^{-\rho t} \log(\tilde{\eta}_t^I \eta_t c_t K_t) dt + (1-\lambda) \mathbb{E} \int_0^{\infty} e^{-\rho t} (\log(\tilde{\eta}_t^H (1-\eta_t) c_t K_t) - b(v_t)) dt \\ \text{s.t. } & c_t = a v_t - \iota_t = \rho \frac{q_t^K}{1 - \vartheta_t}, \quad q_t^K = (1 + \phi \iota_t) \\ & \frac{d\tilde{\eta}_t^I}{\tilde{\eta}_t^I} = \chi_t \frac{1 - \vartheta_t}{\eta_t} \varphi \tilde{\sigma}_t d\tilde{Z}_t, \quad \frac{d\tilde{\eta}_t^H}{\tilde{\eta}_t^H} = (1 - \chi_t) \frac{1 - \vartheta_t}{1 - \eta_t} \tilde{\sigma}_t d\tilde{Z}_t \end{aligned}$$

# Constrained Efficiency

- ▶ Planner's objective can be simplified to a static one

$$\begin{aligned}
 \max_{v_t, \iota_t, \eta_t, \chi_t, \vartheta_t} W_t = & \overbrace{\log(av_t - \iota_t) - (1 - \lambda)b(v_t) + \frac{1}{\rho} \left( \frac{1}{\phi} \log(1 + \phi \iota_t) - \delta \right)}^{\text{aggregate efficiency at } t} \\
 & + \underbrace{\lambda \log(\eta_t) + (1 - \lambda) \log(1 - \eta_t) - \frac{\tilde{\sigma}_t^2}{2\rho} \left[ \lambda \frac{\chi_t^2}{\eta_t^2} \varphi^2 + (1 - \lambda) \frac{(1 - \chi_t)^2}{(1 - \eta_t)^2} \right]}_{\text{distributional efficiency at } t} (1 - \vartheta_t)^2
 \end{aligned}$$

- ▶ Constrained efficient allocation  $v^*(\tilde{\sigma}), \iota^*(\tilde{\sigma}), \eta^*(\tilde{\sigma}), \vartheta^*(\tilde{\sigma}), \chi^*(\tilde{\sigma})$

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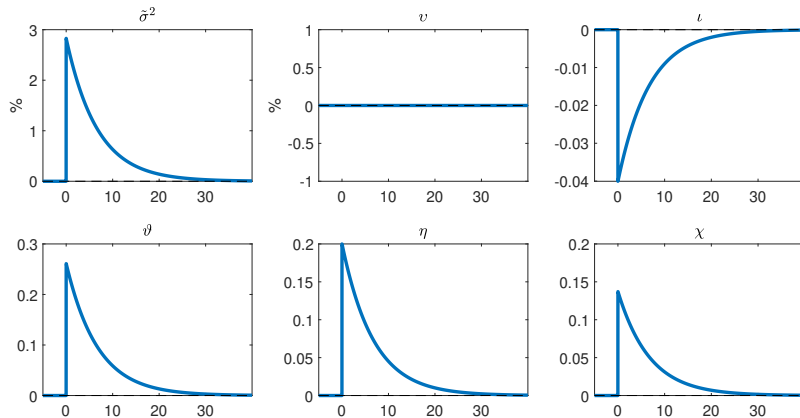
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- ▶ Constrained efficient allocation  $v^*(\tilde{\sigma}), \iota^*(\tilde{\sigma}), \eta^*(\tilde{\sigma}), \vartheta^*(\tilde{\sigma}), \chi^*(\tilde{\sigma})$
- ▶ Optimal allocation:  $1 > \chi^*(\tilde{\sigma}) > \eta^*(\tilde{\sigma}) > \lambda$

# Constrained Efficiency

- ▶ **Proposition 1.** Under some assumption on  $\{\lambda, \varphi\}$ , there exists a unique solution to the planner's problem for  $\eta^*(\tilde{\sigma}_t) > \lambda$  and the constrained efficient allocation has the following properties:
  - ▶ Capital utilization  $v^*(\tilde{\sigma}_t)$  is constant ( $\mu_t^{v,*} = \sigma_t^{v,*} = 0$ )
  - ▶ Intermediaries' wealth and risk shares  $\eta^*(\tilde{\sigma}_t)$  and  $\chi^*(\tilde{\sigma}_t)$  are increasing in  $\tilde{\sigma}_t$
  - ▶ Nominal wealth share  $\vartheta^*(\tilde{\sigma}_t)$  is increasing in  $\tilde{\sigma}_t$
  - ▶ Investment rate  $\iota^*(\tilde{\sigma}_t)$  is decreasing in  $\tilde{\sigma}_t$

## IRF Planner's Solution after $\tilde{\sigma}_t$ -Shock



## Laissez-faire

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- ▶ Goods market clearing:

$$av_t - \iota_t = \rho \left( q_t^K + \frac{\mathcal{B}_t}{\mathcal{P}_t K_t} \right)$$

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- ▶ Sticky prices and no policy response  $\implies$  either inefficient  $v_t$  or  $\iota_t$
- ▶ Policy needs to move nominal wealth in response to an aggregate shock  
(see also Li and Merkel (2025))

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- ▶ Distributional efficiency requires that  $\tilde{\sigma}_t^2 \uparrow \implies \vartheta_t \uparrow$  and  $\eta_t \uparrow$  ( $\sigma_t^\eta > 0$ ,  $\sigma_t^\vartheta > 0$ )

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- ▶ Intermediaries' balance sheet:

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- ▶ Tension: flight-to-safety  $\vartheta_t \uparrow$  redistributes wealth away from intermediaries  $\eta_t \downarrow$
- ▶ Tight link between wealth alloc. across assets ( $\vartheta_t$ ) and agents ( $\eta_t$ ) in CE
- ▶ Policy needs to redistribute wealth in response to an aggregate shock

# Realistic Government

## ► Central bank:

- Sets interest rates  $\underline{i}_t$  and  $i_t$ , reserve requirements  $\underline{\theta}_t^R$
- Issues reserves  $\frac{d\mathcal{R}_t}{\mathcal{R}_t} = \mu_t^{\mathcal{R}} dt + \sigma_t^{\mathcal{R}} dZ_t$
- Holds bonds  $\frac{dL_t^{CB}}{L_t^{CB}} = \mu_t^{L,CB} dt + \sigma_t^{L,CB} dZ_t$

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## ► Fiscal authority:

- Issues long-term bonds  $dL_t^F = \mu_t^{L,F} L_t^F dt$  paying interest  $i^L$ , nominal price  $P_t^L$
  - Levies a range of 'flow' taxes (intermediation, wealth, capital)
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- Motivation: bonds are issued at auctions, CB bond purchases/sales are OMO
- Long-term bond holdings of private agents are  $L_t^I + L_t^H = L_t = L_t^F - L_t^{CB}$
- Distribution across sectors  $\alpha_t = L_t^I / L_t$  is endogenous

# Policy

- ▶ Focus on interest rate and balance sheet policy
- ▶ Fiscal policy operates in the background
- ▶ Balance sheet policy controls the share of long-term bonds in nominal wealth:

$$\vartheta_t^L = \frac{P_t^L L_t}{\mathcal{R}_t + P_t^L L_t} = \frac{P_t^L L_t}{\mathcal{B}_t}$$

- ▶ Interest rate controls sensitivity of bond price to aggregate shocks:

$$\sigma_t^{P^L} = \frac{\partial \log P_t^L}{\partial \log \tilde{\sigma}_t^2} \sigma, \quad P_t^L = \mathbb{E}_t \int_t^\infty e^{-\int_t^\tau (i_s + \sigma_s^{P^L} (\sigma_s^\eta - \sigma_s^\vartheta + \sigma_s^B)) ds} i_\tau^L d\tau$$



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- ▶ Larger CB balance sheet (smaller  $\vartheta^L$ )  $\implies$  more aggressive interest rate policy

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$$\eta_t^* \sigma_t^{\eta,*} = \underbrace{(\eta_t^* - \chi_t^*) \sigma_t^{\vartheta,*}}_{\text{Flight to safety}} + \underbrace{\alpha_t \vartheta_t^* \vartheta^L \sigma_t^{P^L}}_{\text{Direct effect}} + \underbrace{(\chi_t^* - \eta_t^* - \vartheta_t^* \chi_t^*) \vartheta^L \sigma_t^{P^L}}_{\text{Indirect effect}}$$

- ▶ Direct bond revaluation effect:  $\alpha_t \vartheta_t^* \vartheta^L \sigma_t^{P^L} = \frac{L_t^I}{N_t} \sigma_t^{P^L}$
- ▶ Indirect aggregate wealth effect:  $(\chi_t^* - \eta_t^* - \vartheta_t^* \chi_t^*) \vartheta^L \sigma_t^{P^L} = \frac{OE_t^I - N_t^I}{N_t} \vartheta^L \sigma_t^{P^L}$ 
  - ▶ For a fixed  $\vartheta_t = \frac{\mathcal{B}/\mathcal{P}_t}{\mathcal{B}/\mathcal{P}_t + q_t^K K_t}$ ,  $\mathcal{B}_t \uparrow \implies q_t^K \uparrow$
  - ▶ Capital price increase benefits levered intermediaries

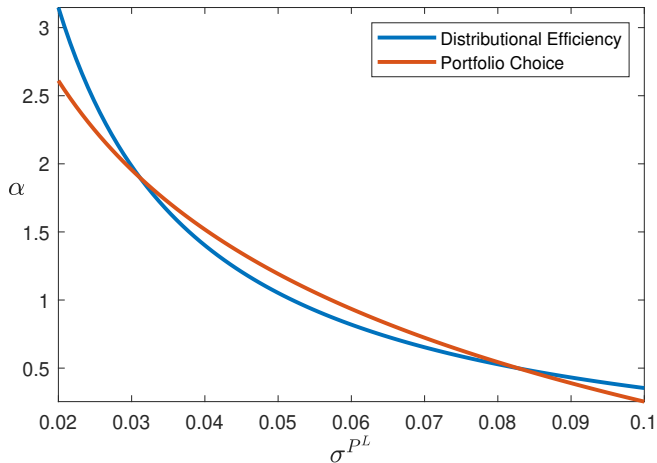
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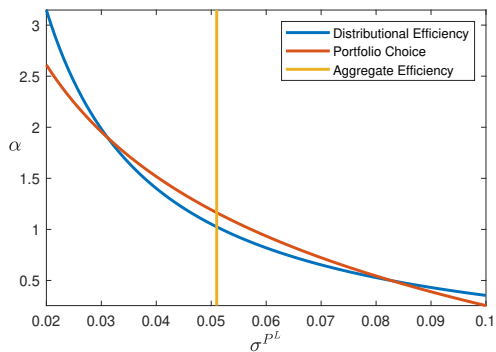
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- ▶ Challenge: endogenous bond distribution  $\alpha_t$
- ▶ Bonds are anti-hedge for intermediaries
- ▶ Intermediaries scale down on bonds if they get more volatile (if  $\sigma_t^{P^L} \uparrow$ )

## Distributional Efficiency Fixing $\vartheta^L$

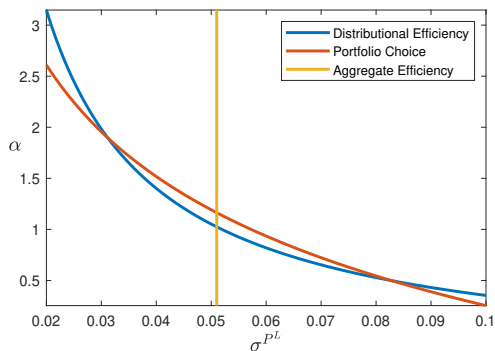


## Aggregate and Distributional Efficiency Fixing $\vartheta^L$



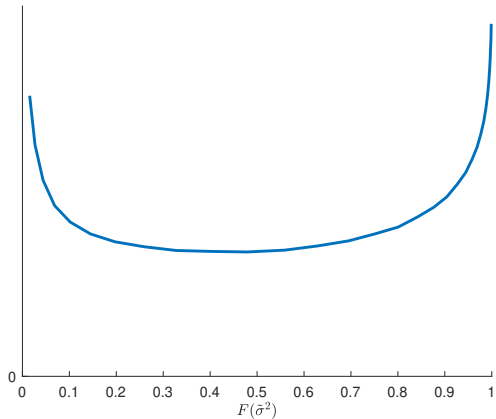


## Aggregate and Distributional Efficiency Fixing $\vartheta^L$



► Requires active balance sheet management!

## Passive balance sheet management: Welfare Loss



- Non-zero welfare loss even around the steady state

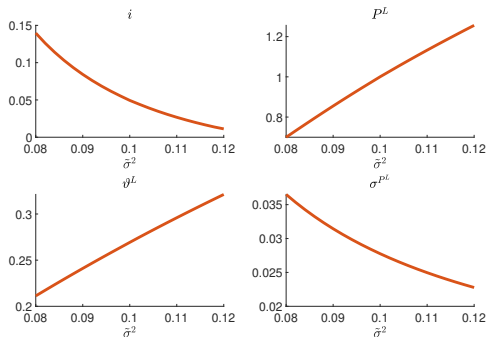
## Existence of an Optimal Policy Mix

- ▶ Existence requires transaction cost function  $t(\nu)$  to be sufficiently steep
  - ▶ Otherwise agents can fully hedge against aggregate risk by freely trading long-term bonds
- ▶ Would a perfectly segmented market help?
  - ▶ No! Perfect segmentation prevents implementation of optimal allocation
  - ▶ It takes away an important 'degree of freedom' from the central bank, making the distribution of LT bonds exogenous and unresponsive to policy
- ▶ Without perfect segmentation, the central bank can manipulate the distribution of duration risk to ensure both aggregate and distributional efficiency
- ▶ Intermediate degree of bond market "segmentation" is needed

# Optimal Policy Over the Cycle

► **Proposition 3.** Let  $\tilde{\sigma}_t^2$  be small. Then, an increase in  $\tilde{\sigma}_t^2$  leads to:

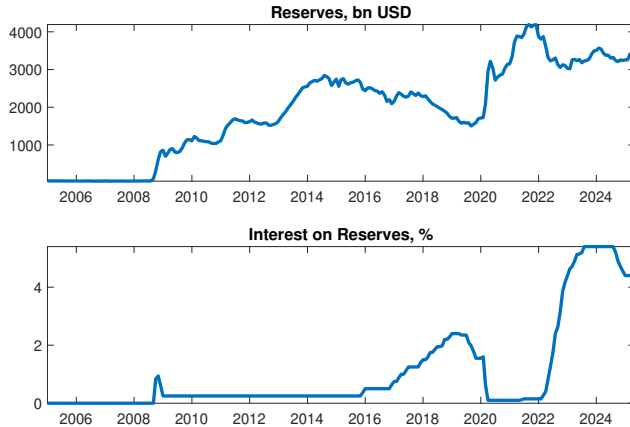
- a cut in the interest rate  $i_t$
- a milder interest rate policy going forward (lower  $\sigma_t^{P^L}$ )
- a rebalancing towards long-term bonds (higher  $\vartheta_t^L$ )



# Summary

- ▶ Macrofinance model to study optimal policy mix
  - ▶ Role for aggregate and distributional efficiencies
- ▶ Preparatory role of balance sheet policies: efficient exposure to future shocks
- ▶ Larger CB balance sheet requires more aggressive interest rate policy subsequently
- ▶ Joint aggregate and distributional efficiency requires active balance sheet management over the cycle

# Motivation



[Back](#)

# Household's Problem

$$\max_{c_t^H, v_t, \iota_t, \nu_t, \theta_t^{D,H}, \theta_t^{L,H}, \theta_t^K, \chi_t} \mathbb{E} \left[ \int_0^\infty e^{-\rho t} (\log(c_t^H) - b(v_t)) dt \right] \quad \text{s.t.}$$

$$\frac{dn_t^H}{n_t^H} = -\frac{c_t^H}{n_t^H} dt + \theta_t^{D,H} dr_t^D + \theta_t^{L,H} dr_t^L + \theta_t^K \left( dr_t^K(v_t, \iota_t, \nu_t) - \chi_t dr_t^{x,H} \right) + \tau_t^H dt$$

$$1 = \theta_t^{D,H} + \theta_t^{L,H} + \theta_t^K(1 - \chi_t) \quad \nu_t \theta_t^{D,H} = \theta_t^K$$

- ▶  $dr_t^K = \left[ \frac{p_t a v_t - \iota_t - \tau_t^K + \mathfrak{d}_t}{q_t^K} - \mathfrak{t}_t(\nu_t) + \mu_t^{q^K} + g(\iota_t) \right] dt + \sigma_t^{q^K} dZ_t + \tilde{\sigma}_t d\tilde{Z}_t$
- ▶  $dr_t^{x,H} = r_t^x dt + \sigma_t^{q^K} dZ_t + \tilde{\sigma}_t d\tilde{Z}_t$
- ▶  $dr_t^D = i_t^D dt + \frac{d(1/\mathcal{P}_t)}{1/\mathcal{P}_t} = [i_t^D - \pi_t] dt$
- ▶  $dr_t^L = \frac{i_t^L}{P_t^L} dt + \frac{d(P_t^L/\mathcal{P}_t)}{P_t^L/\mathcal{P}_t} = \left[ \frac{i_t^L}{P_t^L} + \mu_t^{P^L} - \pi_t \right] dt + \sigma_t^{P^L} dZ_t$

# Intermediary's Problem

$$\max_{c_t^I, \theta_t^{\mathcal{R}}, \theta_t^{L,I}, \theta_t^{D,I}, \theta_t^{x,I}} \mathbb{E} \left[ \int_0^\infty e^{-\rho t} \log(c_t^I) dt \right] \quad \text{s.t.}$$

$$\frac{dn_t^I}{n_t^I} = -\frac{c_t^I}{n_t^I} dt + \theta_t^{\mathcal{R}} dr_t^{\mathcal{R}}(\theta_t^{\mathcal{R}}) + \theta_t^{D,I} dr_t^D + \theta_t^{L,I} dr_t^L + \theta_t^{x,I} dr_t^{x,I} + \tau_t^I dt$$

$$1 = \theta_t^{\mathcal{R}} + \theta_t^{D,I} + \theta_t^{L,I} + \theta_t^{x,I} \quad \theta_t^{\mathcal{R}} \geq \underline{\theta}_t^{\mathcal{R}}$$

- ▶  $dr_t^{\mathcal{R}}(\theta_t^{\mathcal{R}}) = i(\theta_t^{\mathcal{R}})dt + \frac{d(1/\mathcal{P}_t)}{1/\mathcal{P}_t} = \left[ \frac{\theta_t^{\mathcal{R}} i_t + (\theta_t^{\mathcal{R}} - \underline{\theta}_t^{\mathcal{R}}) i_t}{\theta_t^{\mathcal{R}}} - \pi_t \right] dt$
- ▶  $dr_t^{x,I} = (r_t^x + \tau_t^x) dt + \sigma_t^{q^K} dZ_t + \varphi \tilde{\sigma}_t d\tilde{Z}_t$
- ▶  $dr_t^D = i_t^D dt + \frac{d(1/\mathcal{P}_t)}{1/\mathcal{P}_t} = [i_t^D - \pi_t] dt$
- ▶  $dr_t^L = \frac{i_t^L}{P_t^L} dt + \frac{d(P_t^L/\mathcal{P}_t)}{P_t^L/\mathcal{P}_t} = \left[ \frac{i_t^L}{P_t^L} + \mu_t^{P^L} - \pi_t \right] dt + \sigma_t^{P^L} dZ_t$



# Monopolistic Firms

- Monopolistic producers add variety to a common good produced by HH:
  - ▶ Linear technology:  $Y_t^j = y_t^j$ , set prices  $P_t^j$  s.t. Rotemberg frictions:

$$\int_0^\infty \Xi_t^H \left[ \left( \frac{P_t^j}{P_t} \right)^{1-\varepsilon} - p_t(1-\tau^F) \left( \frac{P_t^j}{P_t} \right)^{-\varepsilon} - \frac{\kappa}{2} (\pi_t^j)^2 - T_t^F \right] Y_t dt$$

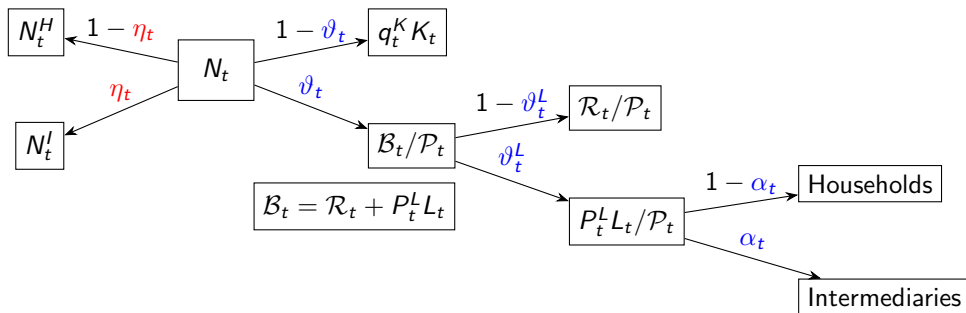
- Perfectly competitive final good producers
  - ▶ Bundle varieties into consumption good using CES aggregator
- NKPC:

$$\frac{\mathbb{E}[d\pi_t]}{dt} = \left( r_t^{f,H} - \frac{\mathbb{E}[dY_t]}{Y_t dt} + \varsigma_t^{C,H} \sigma_t^Y \right) \pi_t - \frac{\varepsilon}{\kappa} \left( p_t(1-\tau) - \frac{\varepsilon-1}{\varepsilon} \right)$$

$$\pi_t = \frac{\varepsilon}{\kappa Y_t} \mathbb{E}_t \int_t^\infty e^{-\int_t^s r_\tau^f d\tau} Y_s \left( p_s(1-\tau) - \frac{\varepsilon-1}{\varepsilon} \right) ds$$

# Net Worth and Risk Distributions

## ► Net worth distribution:



- **Idiosyncratic risk distribution:**  $\chi_t$  held by Intermediaries  
 $1 - \chi_t$  held by Households

# Equilibrium

- ▶ Key variables:  $\tilde{\sigma}_t, \eta_t, v_t, \vartheta_t, P_t^L, \pi_t$
- ▶ Markovian equilibrium with state variables  $S \equiv \{\tilde{\sigma}, \eta, v\}$ :
  - ▶ Laws of motion for  $S$ :

$$d\tilde{\sigma}_t^2 = -b_s(\tilde{\sigma}_t^2 - \tilde{\sigma}_{ss}^2)dt + \sigma\tilde{\sigma}_t^2 dZ_t$$

$$\frac{d\eta_t}{\eta_t} = \mu_t^\eta dt + \sigma_t^\eta dZ_t$$

$$\frac{dv_t}{v_t} = \mu_t^v dt + \sigma_t^v dZ_t$$

- ▶ Policy variables  $\underline{i}(S), i(S), \vartheta^L(S), \underline{\theta}^R(S), \tau^I(S), \tau^X(S), \tau^K(S)$
- ▶ Mappings  $\vartheta(S), P^L(S), \pi(S)$

satisfying agents' optimality and market clearing

## Efficient Consumption & Risk Allocation Only: Implementation

$$\eta_t^* \sigma_t^{\eta,*} = (\eta_t^* - \chi_t^*) \sigma_t^{\vartheta,*} + (\chi_t^* - \eta_t^* + \vartheta_t^* (\alpha_t - \chi_t^*)) \vartheta_t^L \sigma_t^{P^L}$$

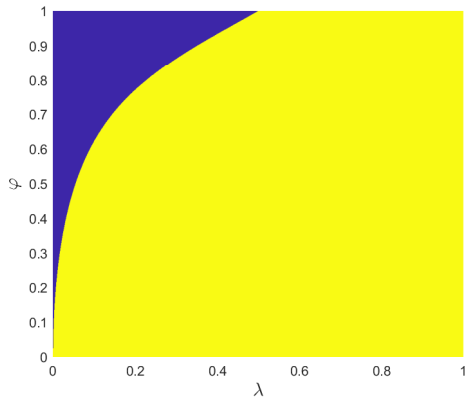
$$\frac{\sigma_t^{\eta,*}}{1 - \eta_t^*} \sigma_t^{P^L} = \nu_t^2 \mathfrak{t}'(\nu_t)$$

$$\nu_t [\chi_t^* - \eta_t^* + \vartheta_t^* (1 - \chi_t^*) - (1 - \alpha_t) \vartheta_t^L \vartheta_t^*] = 1 - \vartheta_t^*$$

Back

## Constrained Efficiency: Properties

$$6\lambda(1-\lambda)(1-\varphi^2)(1-\lambda+\lambda\varphi^2) - (1-2\lambda)\varphi^2 \geq 0$$

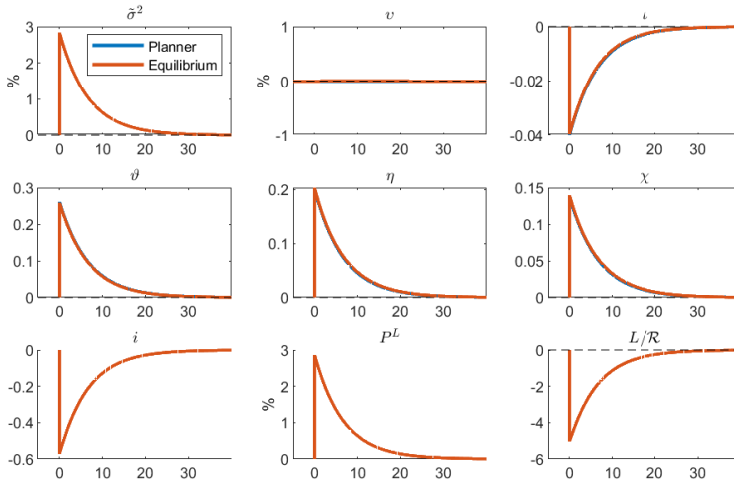


## Consolidated Government

$$\mu_t^{\mathcal{R}} \mathcal{R}_t + P_t^L \mu_t^L L_t + \mathcal{P}_t \tau_t^K K_t = \underline{i}_t \underline{\mathcal{R}}_t + i_t (\mathcal{R}_t - \underline{\mathcal{R}}_t) + i^L L_t - \sigma_t^{P^L} \sigma_t^L P_t^L L_t$$
$$\sigma_t^{\mathcal{R}} \mathcal{R}_t + P_t^L \sigma_t^L L_t = 0$$

Back

# IRF under Full Efficiency



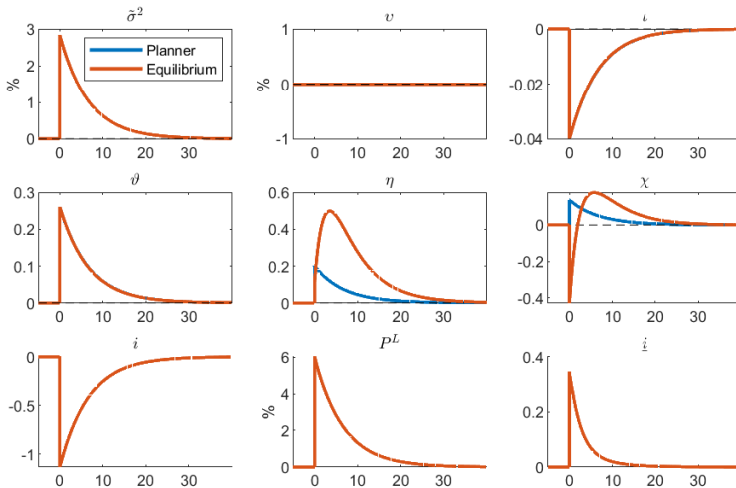
# Production Efficiency Only: Implementation

- ▶  $\vartheta_t$  is an equilibrium 'mapping'
  - $\Rightarrow$  implement  $\vartheta_t^*$  by appropriate capital taxes  $\tau_t^K$  along the equilibrium path
- ▶  $v_t$  is a state variable  $\Rightarrow$  need to ensure  $\mu_t^v = \sigma_t^v = 0 \ \forall t$ 
  - ▶ Drift is targeted by  $i_t$
  - ▶ Volatility loading is targeted by  $i_t$  and  $\vartheta_t^L$
- ▶ From goods market clearing:

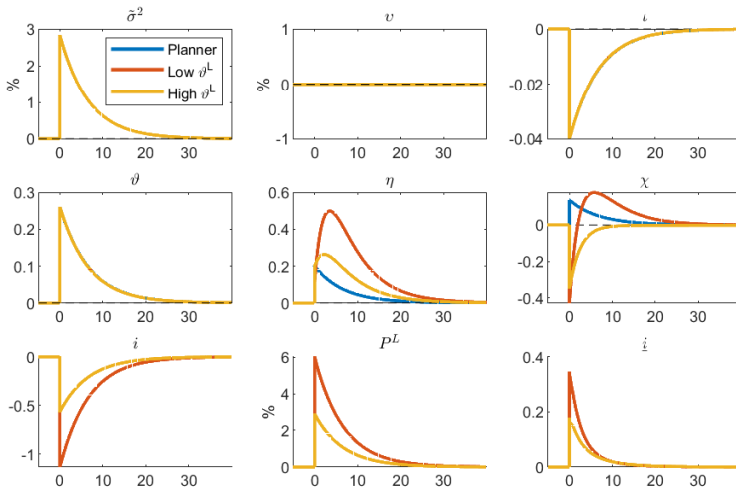
$$av_t = \rho \frac{q_t^B}{\vartheta_t} + \iota_t = \rho \frac{q_t^B}{\vartheta_t} + \frac{q_t^K - 1}{\phi} = \rho \frac{q_t^B}{\vartheta_t} + \frac{q_t^B(1 - \vartheta_t)}{\phi \vartheta_t} - \frac{1}{\phi}$$
$$q_t^B = \frac{B_t}{P_t K_t} \quad B_t = \mathcal{R}_t + P_t^L L_t$$



# IRF under Production Efficiency



# IRF under Production Efficiency: Equivalence



# IRF under Allocative Efficiency: Multiplicity

