

# Macroeconomics

## Lecture 01: Introduction to Macroeconomics

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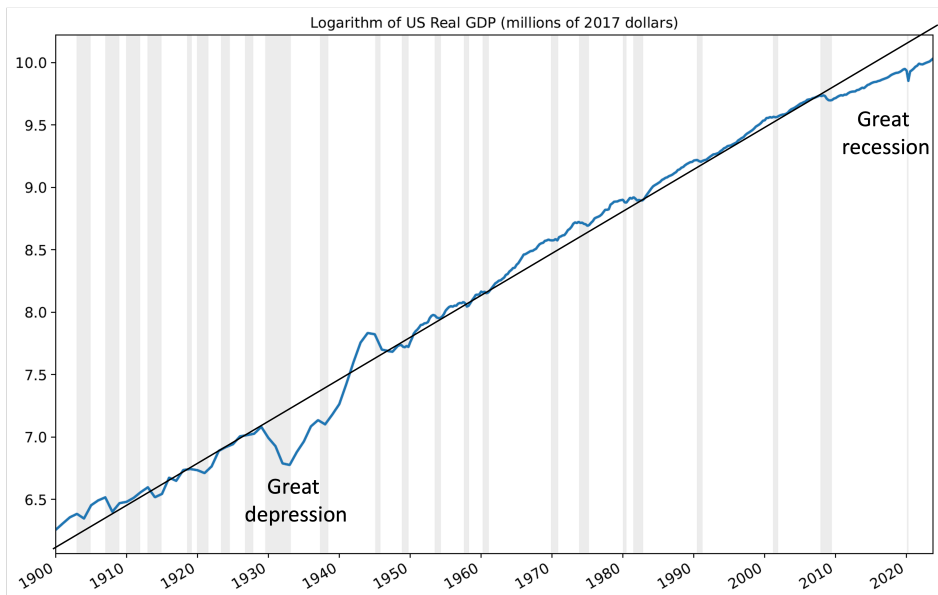
Princeton University

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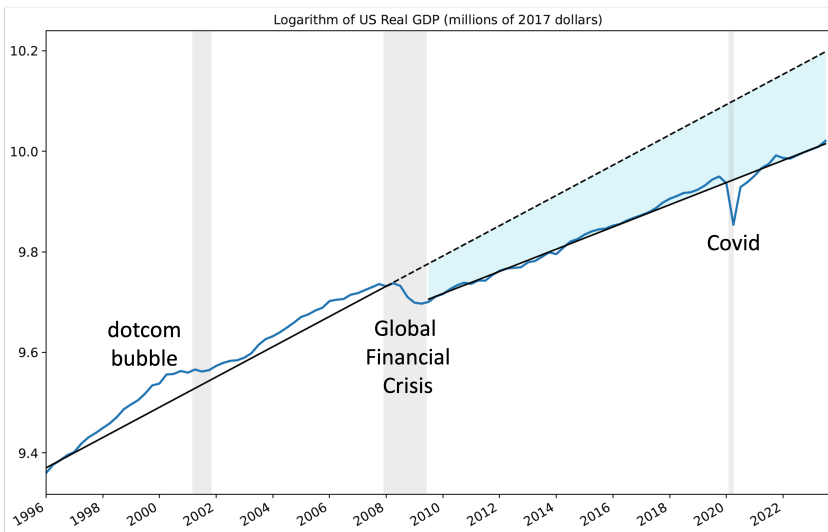
# Introduction to Modern Macro, Money & Finance

- Defining Macrofinance
- Contrasting Different Financial Frictions
- Finance vs. Consumption-Focused Macroeconomics
- Dynamic Amplification, Resilience, Volatility Paradox
- Advantages of Continuous Time Modeling

# Real US GDP in Log: Financial Crises as Resilience Killers



# Real US GDP in Log: Financial Crises as Resilience Killers



Gap in 2023 alone  $\approx$  3 – 4 trillion; Gap over the years (shaded area)

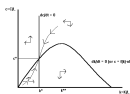
# History of Macro and Finance

## ■ *Verbal Reasoning* (qualitative)

Fisher, Keynes, ...

## Macro

- Growth theory
  - *Dynamic* (cts. time)
  - *Deterministic*



- Introduce stochastic
  - *Discrete time*
    - Brock-Mirman, Stokey-Lucas
    - DSGE models

## Finance

- Portfolio theory
  - *Static*
  - *Stochastic*



## ■ Introduce dynamics

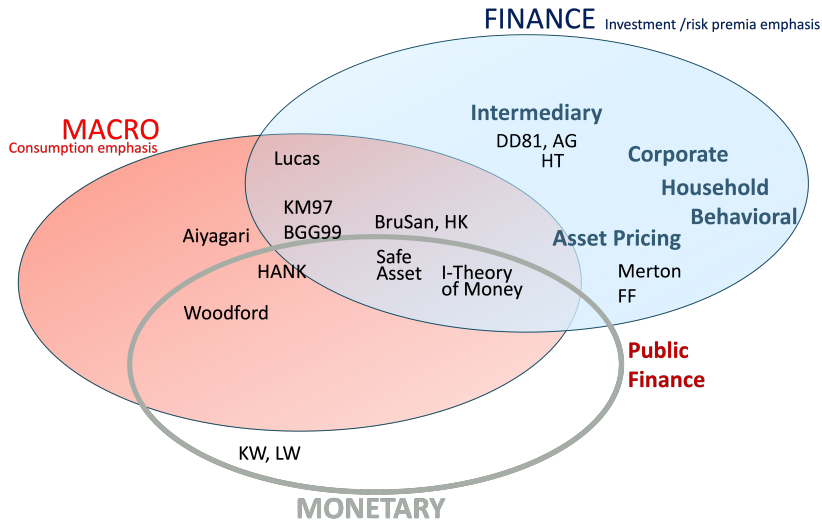
- *Continuous time*
  - Options Black Scholes
  - Term structure CIR
  - Agency theory Sannikov

- Cts. time macro with financial frictions

# What is Macrofinance?

- Macro: aggregate impact (resource allocation and constraint)
- Finance: risk allocation  
financial/contracting frictions, heterogeneous agents  
⇒ institutions, liquidity
- Monetary: inside money creation
- How to design Financial Sector, Gov. bonds, etc.  
to achieve optimal resource and risk allocation
- Topics include:
  - Amplification, percolation of shocks, resilience, financial cycle
  - Financial stability, spillovers, systemic risk measures
  - (Un)conventional central bank policy and balance sheet, maturity structure, CBDC
  - Capital flows

# Macrofinance: More than Intersection of Macro & Finance



# Heterogeneous Agents

- Lending-borrowing/insuring since agents are different

- Poor-rich
- Productive
- Less patient
- Less risk averse
- More optimistic

← Limited direct lending  
due to frictions →

- Rich-poor
- Less productive
- More patient
- More risk averse
- More pessimistic

- Friction: state prices/ $SDF_s$ / $MRS_s$  differ after transactions
- Wealth distribution matters (net worth of subgroups) matters!
- Financial sector is not a veil



# Financial Frictions and Distortions

## ■ Incomplete markets

- “natural” leverage constraint (*BruSan*)
- Costly state verification (*BGG*)

## ■ + Leverage constraints

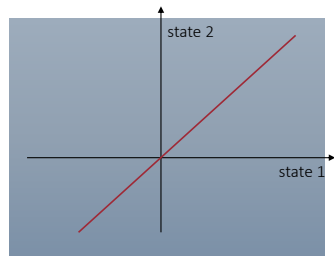
(no “liquidity creation”)

- Exogenous limit (*Bewley/Ayagari*)
- Collateral constraint

- Current price  $D_t \leq q_t k_t$
- Next period's price  $D_t \leq q_{t+1} k_t$  (*KM*)
- Next period's VaR  $D_t \leq \text{VaR}_t(q_{t+1}) k_t$  (*BruPed*)

## ■ Search Friction (*Duffie et al.*)

## ■ Belief Distortions



# Financial Sector

- Financial sector helps to
  - Overcome financing frictions and
  - Channels resources
  - Creates money
- ... but
  - Credit crunch due to adverse feedback loops & liquidity spirals
  - Non-linear dynamics
- New insights to monetary and international economics

# Macro: Finance vs. Consumer Focused

## ■ Portfolio and Investment decision - Macrofinance

- Risk-free rate and risk premia [term-risk, credit risk premia]
- Risk-premia = price of risk \* (exogenous risk + endogenous risk)  
amplification/spirals, runs/sudden
- $\Delta \text{price} = f(\Delta \mathbb{E}[\text{future cash flows}, \Delta \text{risk premia}])$
- Non-linearities are prominent
  - around  $\neq$  away from steady state
- Heterogeneity: wealth distribution across investors (+ consumers)

## ■ Consumption decision

- Demand management [interest rate drives  $c_t$ ]
  - ZLB (liquidity trap)
- Expectation hypothesis, UIP, ... (limited role for time-varying risk premia)
- Heterogeneity: wealth distribution across consumers (with different MPCs)

# Cts.-time Macro: Macrofinance vs HANK

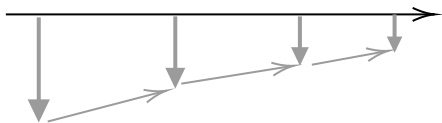
Agents	Heterogenous investor focus - Net worth distribution (often discrete)	Heterogenous consumer focus - Net worth distribution (often cts.)
Tradition:	Finance (Merton) <u>Portfolio and consumption choice</u> <ul style="list-style-type: none"><li>■ Full/global dynamical system</li><li>■ Focused on non-linearities away from steady state (crisis ...)</li><li>■ Length of recession is stochastic</li></ul>	DSGE (Woodford) <u>Consumption choice</u> <ul style="list-style-type: none"><li>■ Zero probability shock</li><li>■ Deterministic transition dynamics back to steady state</li><li>■ Length of recession deterministic</li></ul>
Risk	Risk and Financial Frictions	No aggregate risk (in HANK paper)
Price of risk:	Idiosyncratic and aggregate risk	N/A
Assets:	Capital, money, bonds with different risk profile <ul style="list-style-type: none"><li>■ Risk-return trade-off</li><li>■ Liquidity-return trade-off</li><li>■ Flight-to-safety</li></ul>	All assets are risk free <ul style="list-style-type: none"><li>■ No risk-return trade-off</li><li>■ Liquidity-return trade-off</li></ul>
Money:	Risk and Financial Frictions	Price stickiness

# Overview

- Defining Macrofinance
- Contrasting Different Financial Frictions
- Finance vs. Consumption-Focused Macroeconomics
- Dynamic Amplification, Resilience, Volatility Paradox
  - First Generation Macrofinance: Log-linearize around steady state, zero probability shock followed by deterministic return to steady state (certainty equivalent beliefs)
  - Second Generation Macrofinance: Global Solution, Volatility Dynamics
- Advantages of Continuous Time Modeling

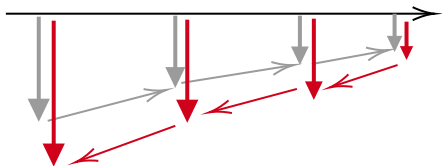
# Persistence and Resilience

- Even in standard real business cycle models, temporary adverse shocks can have long-lasting effects
- Due to feedback effects, persistence is much stronger in models with *financial frictions*
  - Bernanke & Gertler (1989)
  - Carlstrom & Fuerst (1997)
- Negative shocks to net worth exacerbate frictions and lead to lower capital, investment and net worth in future periods



# Persistence Leads to Dynamic Amplification

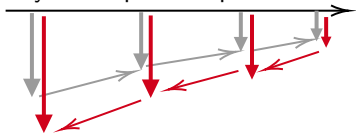
- *Static* amplification occurs because fire-sales of capital from productive sector to less productive sector depress asset prices
  - Importance of *market liquidity* of physical capital
- Dynamic amplification occurs because a temporary shock translates into a persistent decline in output and asset prices
  - Forward      grow net worth via retained earnings
  - Backward    **asset pricing** → **tightens constraints**



# Endogenous Volatility & Volatility Paradox

## ■ Endogenous Risk/Volatility Dynamics in BruSan

### ■ Beyond Impulse responses



■ Input: constant volatility

■ Output: endogenous risk, time varying volatility

⇒ Precautionary savings

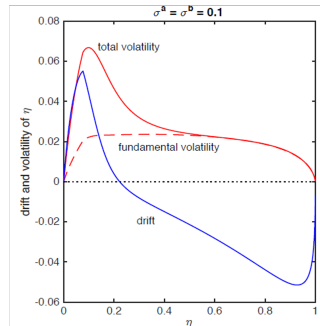
■ Role for money/safe asset

⇒ Nonlinearities in crisis

⇒ Endogenous fat tails, skewness

## ■ Volatility Paradox

- Low exogenous (measured) volatility leads to high build-up of (hidden) endogenous volatility (Minsky' financial instability hypothesis)





# Overview

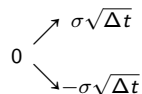
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# Why Continuous Time Modeling?

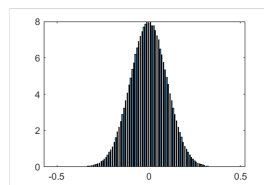
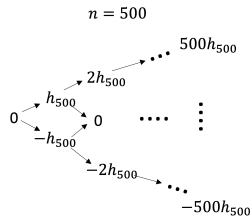
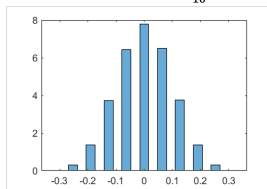
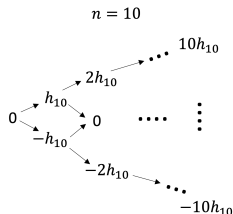
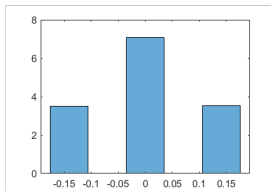
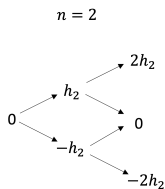
- Time aggregation
  - Data come in different frequency
    - GDP quarterly
    - High frequency financial data
- Consumption
  - Same IES within and across periods
  - Discrete time consumption
    - IES/RA within period =  $\infty$ , but across periods =  $1/\gamma$
- Optimal stopping problems - no interger issues
- Sharp distinction between stock and flow (rate)
  - Beginning of period = end of period wealth
    - E.g. consumption = time-preference rate \* end of period wealth

# Brownian Motion dZ

- Brownian Motion as a binomial tree over  $\Delta t$ .



- More steps with shrinking step size:  $h_n = \sigma\sqrt{\Delta t/n}$

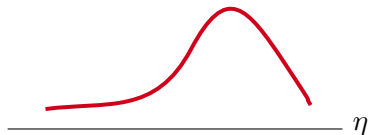


# Itô Processes: Characterization, Skewness over $\Delta t$

- Itô processes ... fully characterized by drift and volatility

$$dX_t = \mu(X_t, t)dt + \sigma(X_t, t)dZ_t$$

- Arithmetic Itô's Process:  $dX_t = \mu_{X,t}dt + \sigma_{X,t}dZ_t$
- Geometric Itô's Process:  $dX_t = \mu_t^X X_t dt + \sigma_t^X X_t dZ_t$
- Characterization for full volatility dynamics on Prob.-Space
  - Discrete time:
    - Probability loading on states
    - Conditional expectations  $\mathbb{E}[X|Y]$  difficult to handle
  - Cts. time: Loading on a Brownian Motion  $dZ_t$  captured by  $\sigma$
- Normal distribution for  $dt$ , yet with skewed distribution for  $\Delta t > 0$



- If  $\sigma_t$  is time-varying
- E.g. from normal- $dt$  to log-normal- $\Delta t$  and vice versa (geometric  $dX_t$ .)

# Continuity of Itô Processes

## ■ Continuous path

- Information arrives continuously “smoothly” - not in lumps
- Implicit assumption: can react continuously to continuous info flow
- Never jumps over a specific point, e.g. insolvency point
- Simplifies numerical analysis:
  - Only need change from grid-point to grid-point (since one never jumps beyond the next grid-points)
- No default risk: Can continuously delever as wealth declines
  - Might embolden investors ex-ante
- Collateral constraint
  - Discrete time:  $b_t R_{t,t+1} \leq \min\{q_{t+1}\} k_t$
  - Cts. time:  $b_t \leq (p_t + \underbrace{dp_t}_{\rightarrow 0}) k_t$

For short-term debt – not for long-term debt ... or if there are jumps

## ■ Levy processes ... with jumps

- Still price of risk \* risk, but not linear

# Conditional Expectations for Itô

- In discrete time: e.g.  $\mathbb{E}_t[V(\eta)]$ 
  - Need function  $V(\eta)$  across all states  $\eta$
  - Simulate  $\eta$  to obtain probability weights for  $\eta$  all realizations

- In continuous time with Itô: 
$$\mathbb{E}[dV(\eta)] = V'(\eta)\mu_\eta dt + \frac{1}{2}V''(\eta)\sigma_\eta^2 dt$$

- Just need the two neighboring grid points instead of the whole function  $\rightarrow V''(\eta)$



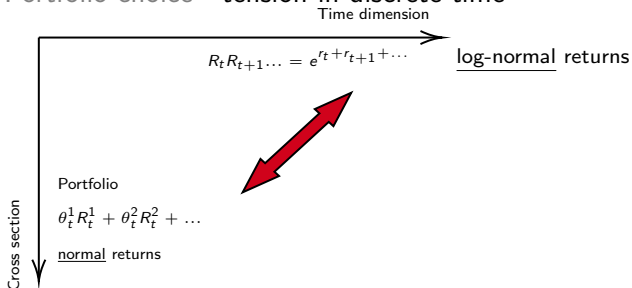
- $V'(\eta)$  is approximated by  $\frac{V(\eta+\Delta)-V(\eta)}{\Delta}$  or  $\frac{V(\eta)-V(\eta-\Delta)}{\Delta}$ ;  
 $V''(\eta)$  by  $\frac{V(\eta+\Delta)-V(\eta)-(V(\eta)-V(\eta-\Delta))}{\Delta^2}$

- Similar for price  $q(\eta)$

Return equations: requires only slope of price function  $q(\eta)$  to determine amplification instead of whole price function across all  $\eta$  in discrete time.

# Dynamic Portfolio Choice in Continuous Time

## ■ Portfolio choice - tension in discrete time



- Linearize kills  $\sigma$ -term, all assets are equivalent
  - 2nd order approximation kills time-varying  $\sigma$
  - Log-linearize à la Campbell-Shiller
- As  $\Delta t \rightarrow 0$  (log) returns converge to normal distribution
- Constantly adjust the approximation point
  - Nice formula for portfolio choice for Ito process

# Consumption Choice & Wealth (Share) Dynamics

- Consumption choice
  - Nice Process
    - Consumption/wealth ratio is constant for log-utility, e.g. for log-utility
$$c_t = \rho N_t$$
    - Beginning = end of period net worth/wealth
- Evolution of state variables wealth (shares)/distribution
  - Nice Characterization
  - Evolution of distributions (e.g. wealth distribution) characterized by Kolmogorov Forward Equation (Fokker-Planck equation)



# Conclusion & Takeaways

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