Macro, Money and Finance

Markus Brunnermeier and Yuliy Sannikov

Princeton University

Motivation

- Aim: Bridge the gap between
  - Macro/monetary research
  - Finance research

- Financial sector helps to
  - overcome financing frictions and
  - channels resources
  - creates money

  … but
  - Credit crunch due to
    adverse feedback loops & liquidity spirals
    - Non-linear dynamics
- New insights to monetary and international economics

Output (gap)

- Price stability
  Monetary policy
- Financial stability
  Macroprudential policy
- Fiscal debt sustainability
  Fiscal

- Short-term interest
- Policy rule (terms structure)

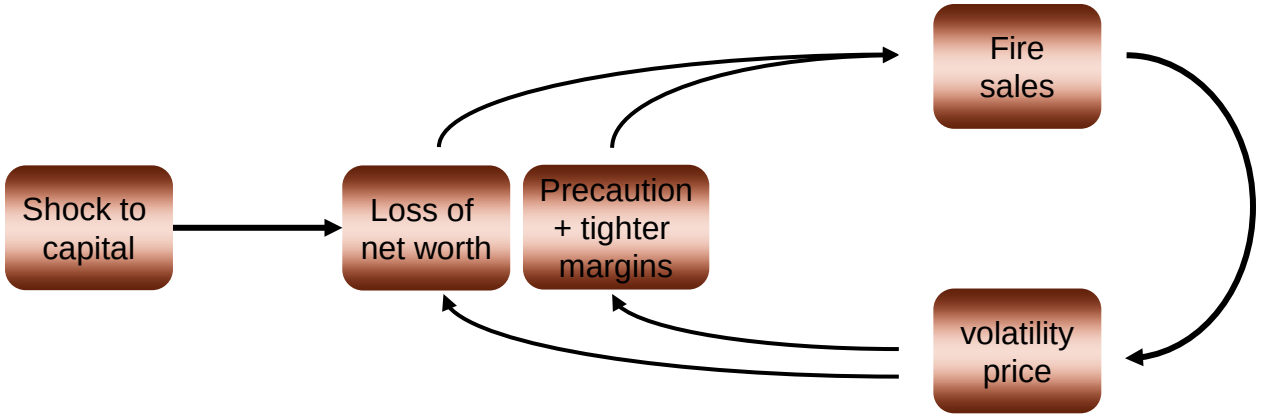
inter-action

- Reserve requirements
- Capital/liquidity requirements
- Collateral policy Margins/haircuts
- Capital controls

inter-action

Systemic risk – a broad definition

- Systemic risk build-up during (credit) bubble
  … and materializes in a crisis
  - "Volatility Paradox" → contemp. measures inappropriate
- Spillovers/contagion – externalities
  - Direct contractual: domino effect (interconnectedness)
  - Indirect: price effect (fire-sale externalities)
    credit crunch, liquidity spirals



  - *Adverse GE response* ⇒ amplification, persistence

preventive

crisis management

Minsky moment – Wile E. Coyote Effect

Methodology – relation to finance

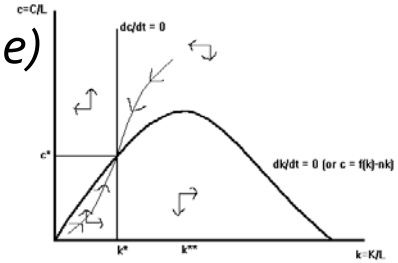
timeline

- *Verbal Reasoning* *(qualitative)*

Fisher, Keynes, …

Macro

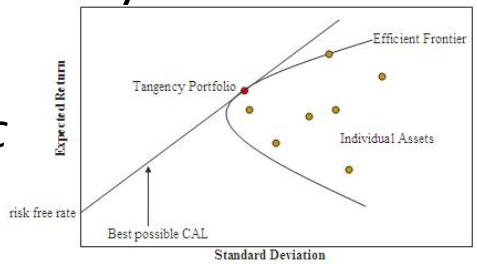
- Growth theory
  - *Dynamic (cts. time)*
  - *Deterministic*



- Introduce stochastic
  - *Discrete time*
    - Brock-Mirman, Stokey-Lucas
    - DSGE models

Finance

- Portfolio theory
  - *Static*
  - *Stochastic*



- Introduce dynamics
  - *Continuous time*
    - Options Black Scholes
    - Term structure CIR
    - Agency theory Sannikov

- Cts. time macro with financial frictions

Heterogeneous agents + frictions

- Lending-borrowing/insuring since agents are different

▪ Poor-rich ▪ Productive ▪ Less patient ▪ Less risk averse ▪ More optimistic	← Limited direct lending due to frictions	▪ Rich-poor ▪ Less productive ▪ More patient ▪ More risk averse ▪ More pessimistic

- Friction → $p_s MRS_s$ different even after transactions
- **Wealth distribution matters!** (net worth of subgroups)
- **Financial sector is not a veil**

Liquidity – Persistence & Amplification

Markus Brunnermeier and Yuliy Sannikov

Princeton University

Liquidity Concepts

- Financial instability arises from the fragility of liquidity

A	L
Technological liquidity ▪ Reversibility of investment **Market liquidity** ▪ Specificity of capital Price impact of capital sale	**Funding liquidity** ▪ Maturity structure of debt ▪ Can't roll over short term debt ▪ Sensitivity of margins ▪ Margin-funding is recalled

Liquidity ~~Maturity~~ mismatch

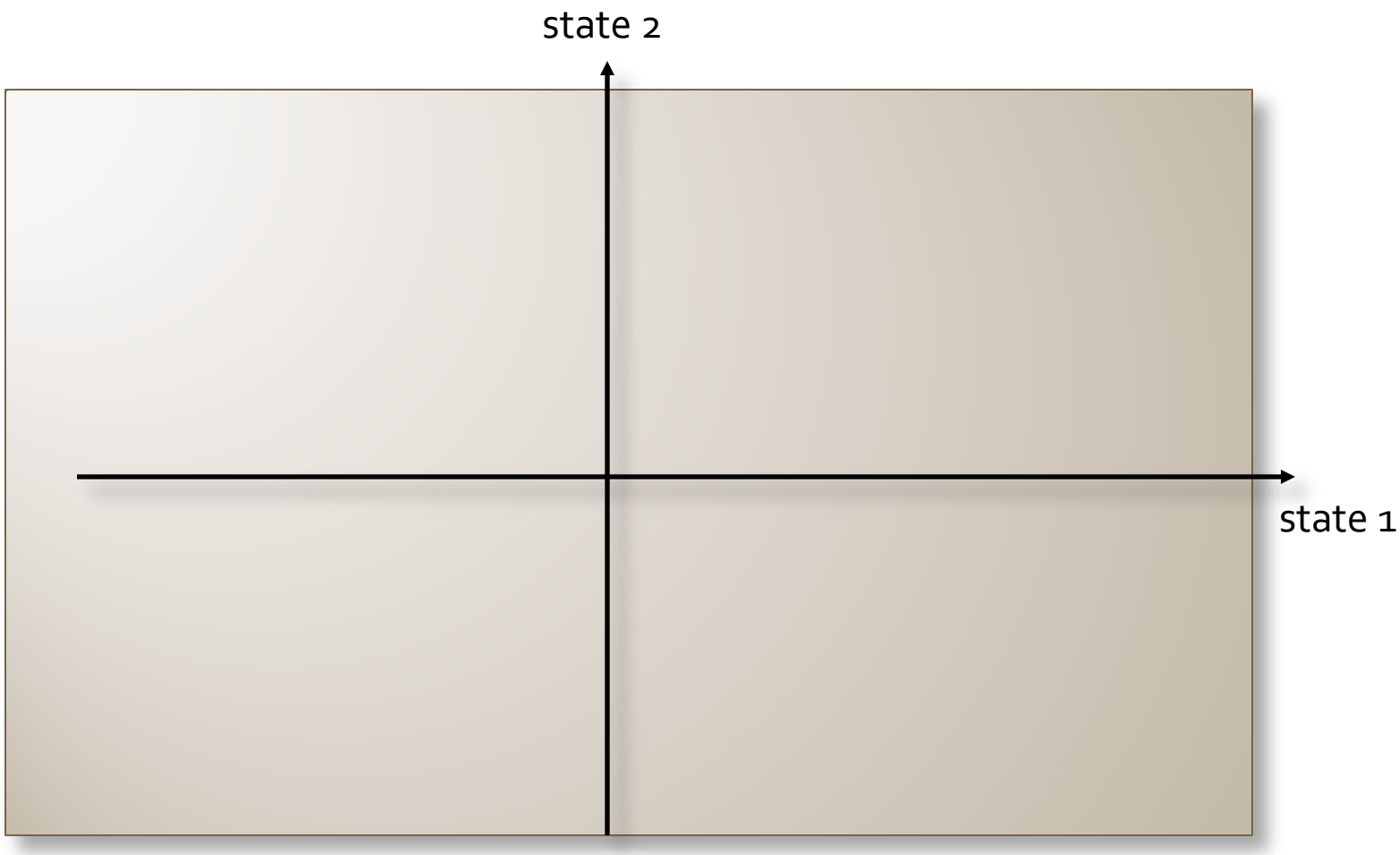
- *Liquidity mismatch* determines severity of amplification

Types of Funding Constraints

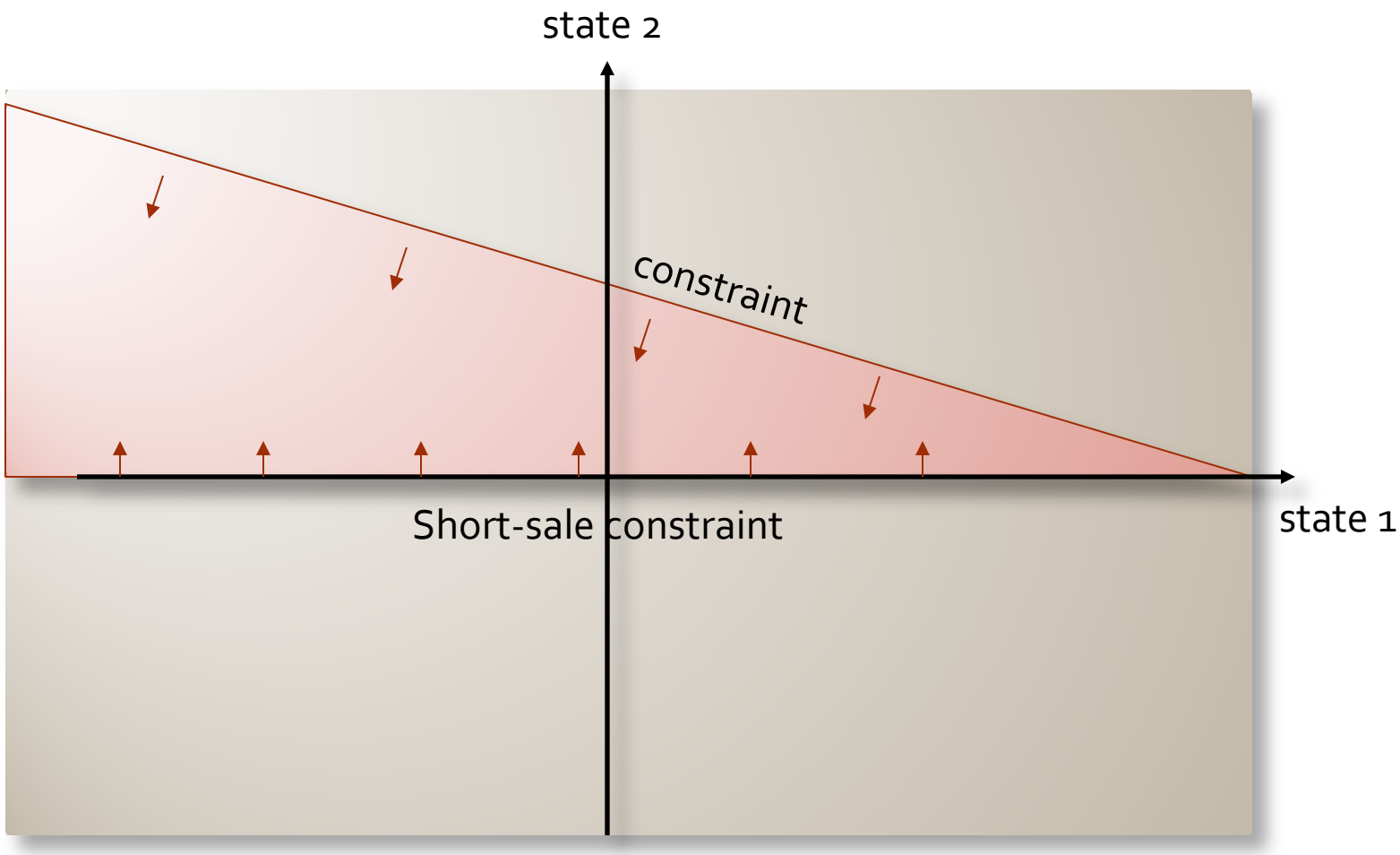
- Equity constraint
  - "Skin in the game constraint"
- + Debt constraints
  - Costly state verification a la Townsend — CF, BGG
    - Borrowing cost increase as net worth drops
  - Collateral/leverage/margin constraints — KM, BP, G
    - Quantity constraint on borrowing
    - Incomplete contracts a la Hart-Moore
    - Commitment problem
    - Credit rationing a la Stiglitz-Weiss
  - Not binding (precautionary buffer) — BruSan, He-Krishnamurthy

Comment: Constraints vs. incomplete markets

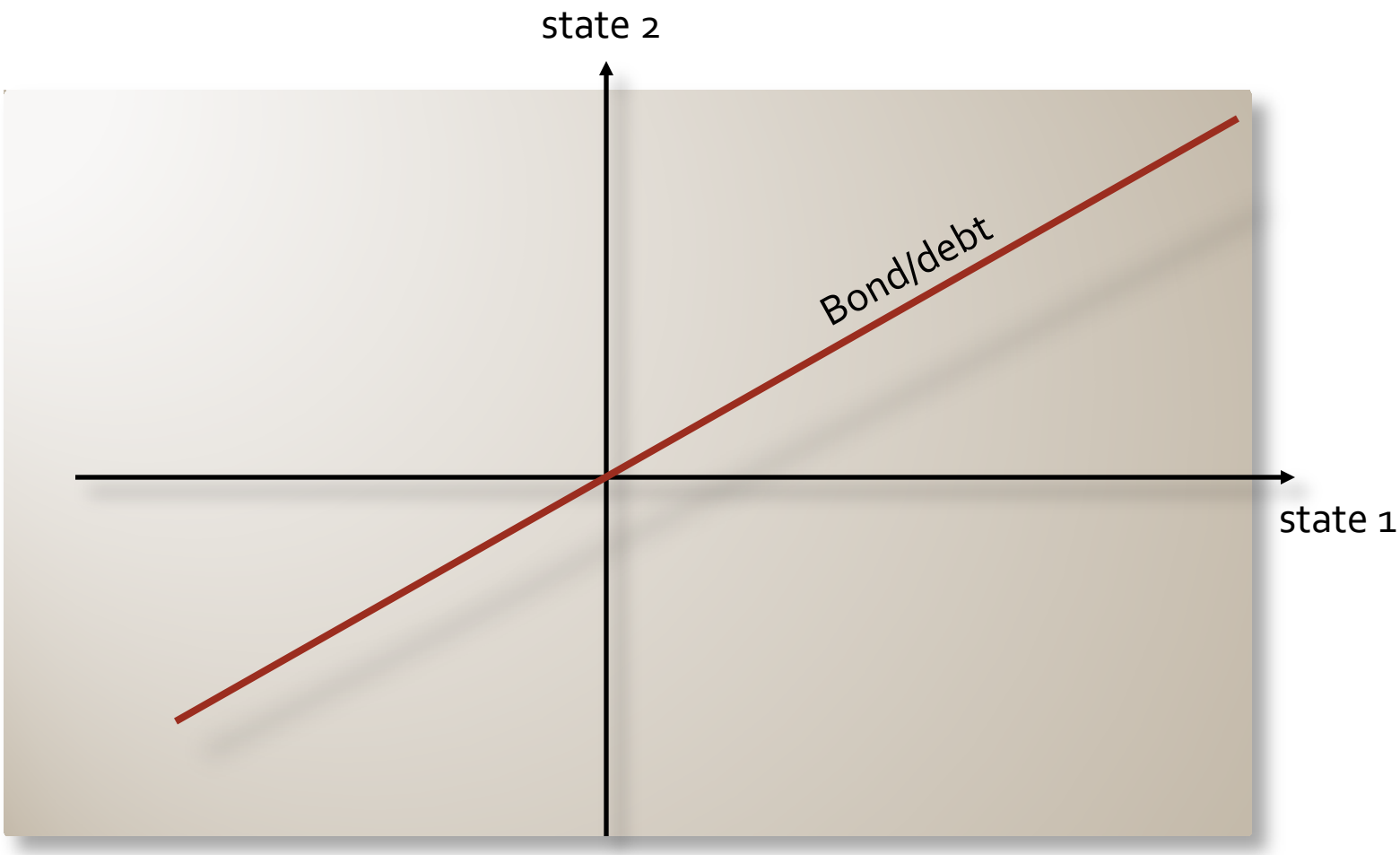
Constraints vs. Incomplete Markets



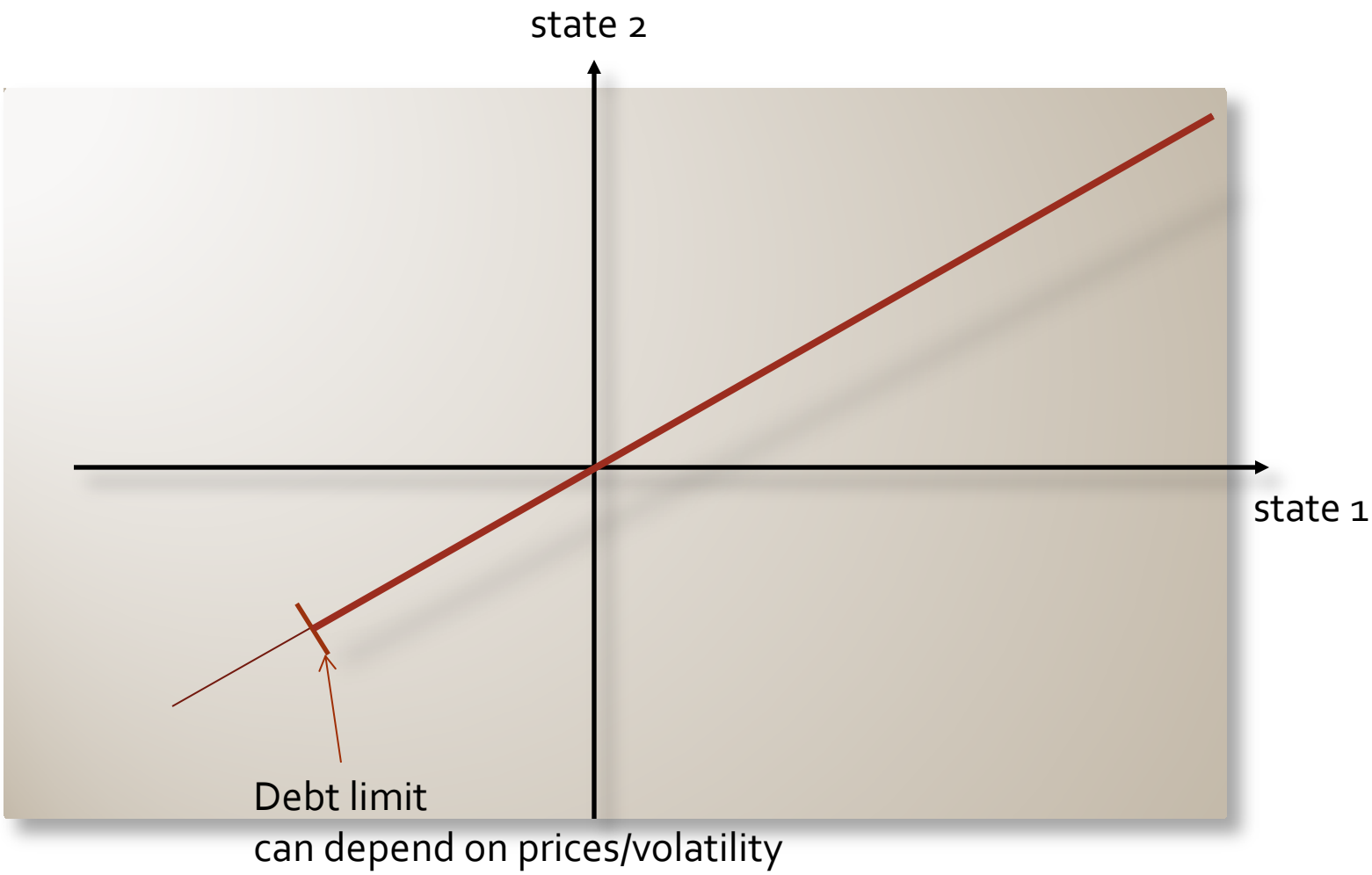
Constraints vs. Incomplete Markets



Constraints vs. Incomplete Markets



Constraints & Incomplete Markets

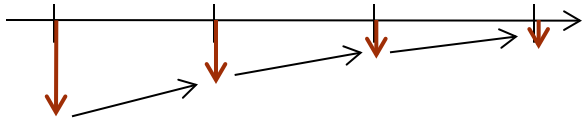


Macro-literature on Frictions

1. Net worth effects:
   a. Persistence: Carlstrom & Fuerst
   b. Amplification: Bernanke, Gertler & Gilchrist
      "Kocherlakota critique"
2. Volatility effects: impact credit quantity constraints
   a. Instability: Brunnermeier & Sannikov
   b. Margin spirals : Brunnermeier & Pederson
   c. Endogenous constraints: Geanakoplos
3. Demand for liquid assets & Bubbles – "self insurance"
   a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,…
4. Financial intermediaries & Theory of Money

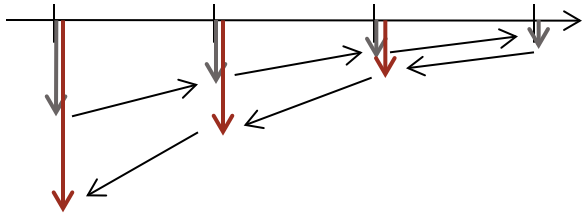
Amplification & Instability - Overview

- Bernanke & Gertler (1989), Carlstrom & Fuerst (1997)
  - Perfect (technological) liquidity, but persistence
  - Bad shocks erode net worth, cut back on investments, leading to low productivity & low net worth of in the next period



Amplification & Instability - Overview

- Bernanke & Gertler (1989), Carlstrom & Fuerst (1997)
  - Perfect (technological) liquidity, but persistence
  - Bad shocks erode net worth, cut back on investments, leading to low productivity & low net worth of in the next period



- Kiyotaki & Moore (1997), BGG (1999)
  - Technological/market illiquidity
  - KM: Leverage bounded by margins; BGG: Verification cost (CSV)
  - Stronger amplification effects through prices (low net worth reduces leveraged institutions' demand for assets, lowering prices and further depressing net worth)
- Brunnermeier & Sannikov (2010)
  - Instability, volatility dynamics, volatility paradox, Kocherlakota critique
- Brunnermeier & Pedersen (2009), Geanakoplos
  - Volatility interaction with margins/haircuts (leverage)

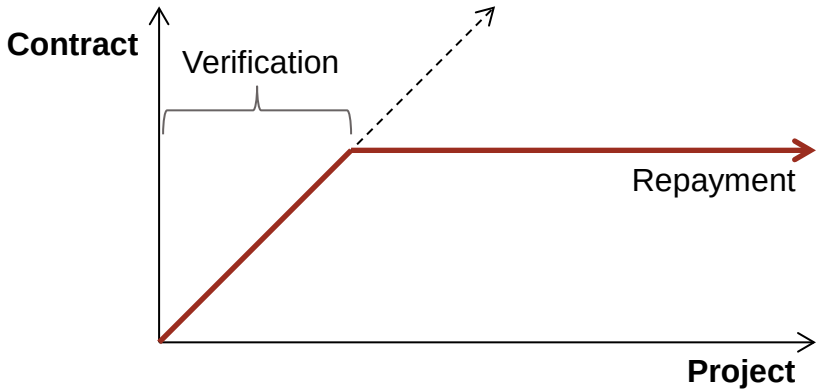
Persistence

- Even in standard real business cycle models, temporary adverse shocks can have long-lasting effects
- Due to feedback effects, persistence is much stronger in models with *financial frictions*
  - Bernanke & Gertler (1989)
  - Carlstrom & Fuerst (1997)
- Negative shocks to net worth exacerbate frictions and lead to lower capital, investment and net worth in future periods

Jump

Costly State Verification

- Key friction in previous models is <u>costly state verification</u>, i.e. CSV, a la Townsend (1979)
- Borrowers are subject to an idiosyncratic shock
  - Unobservable to lenders, but can be verified at a cost
- Optimal solution is given by a contract that resembles standard debt

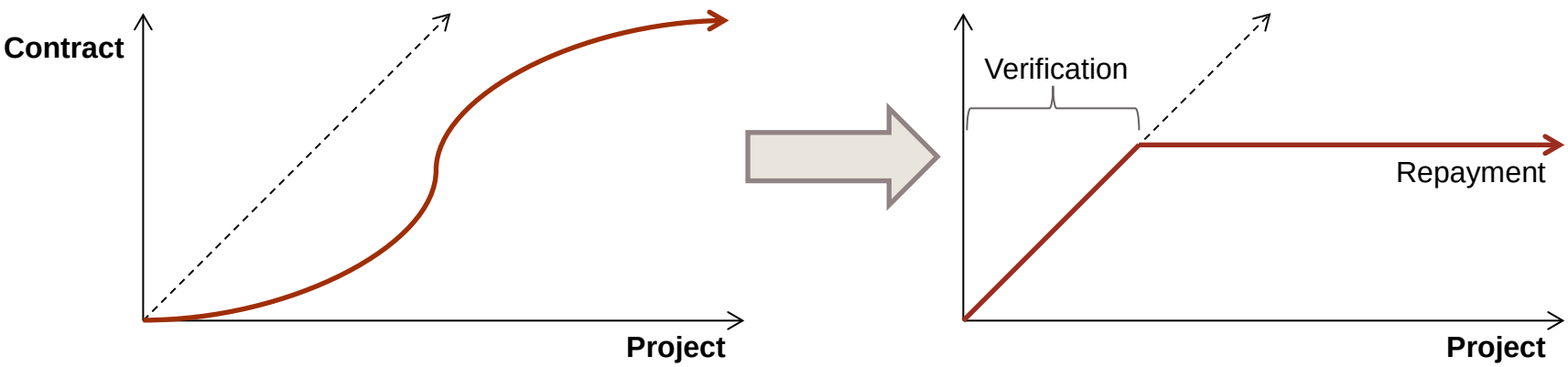


CSV: Contracting

- Competitive market for capital
  - Lender's expected profit is equal to zero
  - Borrower's optimization is equivalent to minimizing expected verification cost
- Financial contract specifies:
  - Debt repayment for each reported outcome
  - Reported outcomes that should be verified

CSV: Optimal Contract

- Incentive compatibility implies that
  - Repayment outside of VR is constant
  - Repayment outside of VR is weakly greater than inside
- Maximizing repayment in VR reduces the size and thus the expected verification cost



Carlstrom & Fuerst

- Output is produced according to $Y_t = A_t f(K_t)$
- Fraction η of entrepreneurs and $1 - \eta$ of households
  - Only entrepreneurs can create new capital from consumption goods
- Individual investment yields ωi_t of capital
  - Shock is given by $\omega \sim G$ with $E[\omega] = 1$
  - This implies consumption goods are converted to capital one-to-one in the *aggregate*
  - *No technological illiquidity!*

CF: Costly State Verification

- Households can verify ω at cost μi_t
  - Optimal contract is debt with audit threshold $\overline{\omega}$
  - Entrepreneur with net worth n_t borrows $i_t - n_t$ and repays $\min\{\omega_t, \overline{\omega}\} \times i_t$
- Auditing threshold is set by HH breakeven condition
  - $\left[\int_0^{\overline{\omega}} (\omega - \mu) dg(\omega) + \left(1 - G(\overline{\omega})\right)\overline{\omega}\right] i_t q_t = i_t - n_t$
  - Here, q_t is the price of capital
- No positive interest (within period borrowing) and no risk premium (no aggregate investment risk)

CF: Persistence & Dampening

- Negative shock in period t decreases N_t
  - This increases financial friction and decreases I_t
- Decrease in capital supply leads to
  - Lower capital: K_{t+1}
  - Lower output: Y_{t+1}
  - Lower net worth: N_{t+1}
  - Feedback effects in future periods $t + 2, \ldots$
- Decrease in capital supply also leads to
  - Increased price of capital q_t
  - Dampening effect on propagation of net worth shock

Dynamic Amplification

- Bernanke, Gertler and Gilchrist (1999) introduce *technological illiquidity* in the form of nonlinear adjustment costs to capital
- Negative shock in period t decreases N_t
  - This increases financial friction and decreases I_t
- In contrast to the dampening mechanism present in CF, now decrease in **capital demand** (not supply) leads to
  - Decreased price of capital due to adjustment costs
  - *Amplification* effect on propagation of net worth shock

Bernanke, Gertler & Gilchrist

- BGG assume separate investment sector
  - This separates entrepreneurs' capital decisions from adjustment costs
- $\Phi(\cdot)$ represents *technological illiquidity*
  - Increasing and concave with $\Phi(0) = 0$
  - $K_{t+1} = \Phi\left(\frac{I_t}{K_t}\right) K_t + (1-\delta)K_t$
- FOC of investment sector
  - $\max_{I_t}\{q_t K_{t+1} - I_t\} \Rightarrow q_t = \Phi'\left(\frac{I_t}{K_t}\right)^{-1}$

jump to KM97

BGG: Entrepreneurs

- Entrepreneurs alone can hold capital used in production (of consumption good)
- At time t, entrepreneurs purchase capital for $t+1$
  - To purchase k_{t+1}, an entrepreneur borrows $q_t k_{t+1} - n_t$
  - Here, n_t represents entrepreneur net worth
- Assume gross return to capital is given by ωR_{t+1}^k
  - Here $\omega \sim G$ with $E[\omega] = 1$ and ω i.i.d.
  - R_{t+1}^k is the endogenous aggregate equilibrium return

BGG: Persistence & Amplification

- Shocks to net worth N_t are persistent
  - They affect capital holdings, and thus N_{t+1}, …
- *Technological illiquidity* for capital "demanders" no introduces amplification effect
  - Decrease in capital leads to reduced price of capital from $q_t = \Phi'\left(\frac{I_t}{K_t}\right)^{-1}$
  - Lower price of capital further decreases net worth

Kiyotaki & Moore 97

- Kiyotaki, Moore (1997) adopt a
  - collateral constraint instead of CSV
  - *market illiquidity* – second best use of capital
- Output is produced in two sectors, differ in productivity
- Aggregate capital is fixed, resulting in extreme *technological illiquidity*
  - Investment is completely irreversible
- Durable asset has two roles:
  - Collateral for borrowing
  - Input for production

Jump

KM: Amplification

- *Static* amplification occurs because fire-sales of capital from productive sector to less productive sector depress asset prices
  - Importance of *market liquidity* of physical capital
- *Dynamic* amplification occurs because a temporary shock translates into a persistent decline in output and asset prices

KM: Agents

- Two types of infinitely-lived risk neutral agents
- Mass η of productive agents
  - Constant-returns-to-scale production technology yielding $y_{t+1} = ak_t$
  - Discount factor $\beta < 1$
- Mass $1 - \eta$ of less productive agents
  - Decreasing-returns-to-scale production $y_{t+1} = F(k_t)$
  - Discount factor $\underline{\beta} \in (\beta, 1)$

KM: Frictions

- Since productive agents are less patient, they will want to borrow b_t from less productive agents
  - However, friction arises in that each productive agent's technology requires *his* individual human capital
  - Productive agents cannot pre-commit human capital
- This results in a collateral constraint

$$Rb_t \leq q_{t+1}k_t$$

  - Productive agent will never repay more than the value of his asset holdings, i.e. collateral

KM: Demand for Assets

- Since there is no uncertainty, a *productive agent* will borrow the maximum quantity and will not consume any of the output
  - Budget constraint: $q_t k_t - b_t \leq (a + q_t)k_{t-1} - Rb_{t-1}$
  - Demand for assets: $k_t = \frac{1}{q_t - \frac{q_{t+1}}{R}}[(a + q_t)k_{t-1} - Rb_{t-1}]$
- Unproductive agents are not borrowing constrained
  - $R = \underline{\beta}^{-1}$ and asset demand is set by equating margins
  - Demand for assets: $R = \frac{\underline{F}'(\underline{k}_t) + q_{t+1}}{q_t}$

Rewritten to $\frac{1}{R}\underline{F}'(\underline{k}_t) = q_t - \frac{1}{R}q_{t+1}$

KM: Equilibrium

- With fixed supply of capital, market clearing requires $\eta K_t + (1-\eta)\underline{K_t} = \bar{K}$
  - This implies $M(K_t) \equiv \frac{1}{R}\underline{F}'\left(\frac{\bar{K}-\eta K_t}{1-\eta}\right) = q_t - \frac{1}{R}q_{t+1}$
  - Note that $M(\cdot)$ is increasing
- Iterating forward, we obtain: $q_t = \sum_{s=0}^{\infty}\frac{1}{R^s}M(K_{t+s})$

KM: Steady State

- In steady state, productive agents use tradable output a to pay interest on borrowing:
- This implies that steady state price q^* must satisfy:
  - $q^* - \frac{1}{R} q^* = a$
- Further, steady state capital K^* must satisfy:
  - $\frac{1}{R} \underline{F}' \left(\frac{\bar{K} - \eta K^*}{1 - \eta} \right) = a$
  - This reflects inefficiency since marginal products correspond only to *tradable* output as opposed to total $a + c$, where c is non-tradable fraction

KM: Productivity Shock

- Log-linearized deviations around steady state:
  - Unexpected one-time shock that reduces production of all agents by factor $1-\Delta$
- %-change in assets for given change in asset price:
  - $\widehat{K}_t = -\frac{\xi}{1+\xi}\left(\Delta + \frac{R}{R-1}\hat{q}_t\right),\ \widehat{K}_{t+s} = \frac{\xi}{1+\xi}\widehat{K}_{t+s-1}$
  - $\frac{1}{\xi} = \frac{d\log M(K)}{d\log K}\Big|_{K=K^*}$ (elasticity)
- Reduction in assets comes from two shocks:
  - Lost output Δ
  - Capital losses on previous assets $\frac{R}{R-1}\hat{q}_t$, amplified by leverage
  - $\frac{\xi}{1+\xi}$ terms dampens effect since asset can reallocated

KM: Productivity Shock

- Change in price for given change in assets:
  - Log-linearize the equation $q_t = \sum_{s=0}^{\infty} \frac{1}{R^s} M(K_{t+s})$
  - This provides: $\hat{q}_t = \frac{1}{\xi} \frac{R-1}{R} \sum_{s=0}^{\infty} \frac{1}{R^s} \hat{K}_{t+s}$
- Combining equations:

Multiplier	static	dynamic
$\hat{K}_t =$	$-\Delta$	$-\frac{1}{(\xi+1)(R-1)}\Delta$
$\hat{q}_t =$	$-\frac{(R-1)}{R}\frac{1}{\xi}\Delta$	$-\frac{1}{R}\frac{1}{\xi}\Delta$

  - Static effect results from assuming $q_{t+1} = q^*$

"Kocherlakota critique"

- Amplification for negative shocks differs from positive shocks
  - In Kocherlakota (2000) optimal scale of production (positive shock does not lead to expansion)
- Amplification is quantitatively too small
  - Capital share is only 1/3 and hence GDP is too small
  - Cordoba and Ripoll (2004)
    - Needs sizeable capital share plus
    - Low intertemporal substitution

Macro-literature on Frictions

1. Net worth effects:
   a. Persistence: Carlstrom & Fuerst
   b. Amplification: Bernanke, Gertler & Gilchrist
      "Kocherlakota critique"
2. Volatility effects: impact credit quantity constraints
   a. Instability: Brunnermeier & Sannikov
   b. Margin spirals : Brunnermeier & Pederson
   c. Endogenous constraints: Geanakoplos
3. Demand for liquid assets & Bubbles – "self insurance"
   a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,…
4. Financial intermediaries & Theory of Money

BruSan10: Instability & Non-Linear Effects

- Previous papers only considered log-linearized solutions around steady state
- Brunnermeier & Sannikov (2010) build a continuous time model to study full dynamics
  - Show that financial system exhibits inherent instability due to highly non-linear effects
  - These effects are asymmetric and only arise in the downturn
- Agents choose a *capital cushion*
  - Mitigates moderate shocks near steady state
  - High volatility away from steady state

Macro-literature on Frictions

1. Net worth effects:
   a. Persistence: Carlstrom & Fuerst
   b. Amplification: Bernanke, Gertler & Gilchrist
      "Kocherlakota critique"
2. Volatility effects: impact credit quantity constraints
   a. Instability: Brunnermeier & Sannikov
   b. Margin spirals : Brunnermeier & Pederson
   c. Endogenous constraints: Geanakoplos
3. Demand for liquid assets & Bubbles – "self insurance"
   a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,…
4. Financial intermediaries & Theory of Money

Credit Rationing – Quantity Rationing

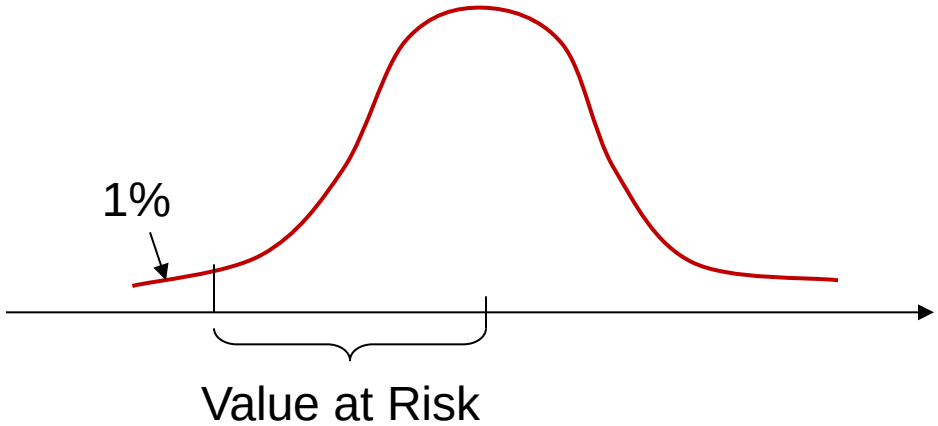
- Credit rationing refers to a failure of market clearing in credit
  - In particular, an excess demand for credit that fails to increase market interest rate
  - Pool of loan applicants worsens
  - Stiglitz & Weiss (1981) show how asymmetric information on risk can lead to credit rationing

Brunnermeier-Pedersen: Margin Spiral

- For collateralized lending, debt constraints are directly linked to the volatility of collateral
  - Constraints are more binding in volatile environments
  - Feedback effect between volatility and constraints
- These margin spirals force agents to delever in times of crisis
  - Collateral runs counterparty bank run
  - Multiple equilibria

BP: Margins – Value at Risk (VaR)

- How are margins set by brokers/exchanges?
  - **Value at Risk**: $\Pr(-(p_{t+1} - p_t) \geq m) = 1\% = \pi$



BP: Leverage and Margins

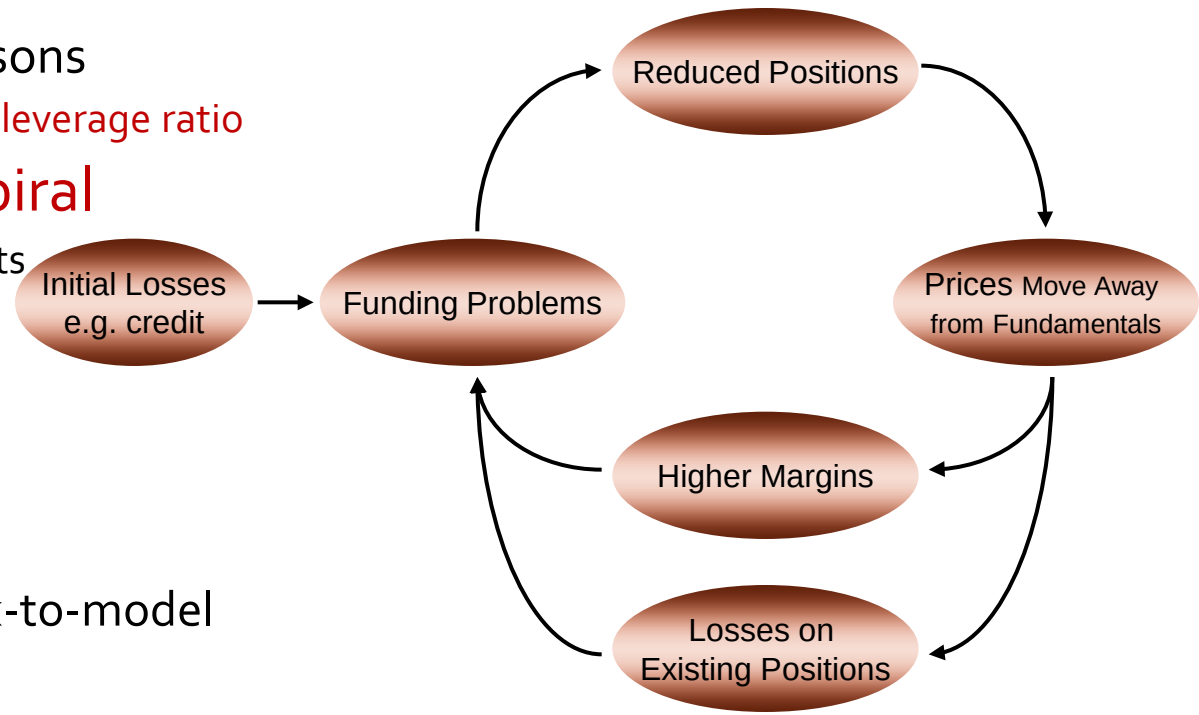
- Financing a *long position* of $x^{j+}_t>0$ shares at price $p^j_t=100$:
  - Borrow \$90\$ dollar per share;
  - Margin/haircut: $m^{j+}_t=100-90=10$
  - Capital use: \$10 x^{j+}_t
- Financing a *short position* of $x^{j-}_t>0$ shares:
  - Borrow securities, and lend collateral of 110 dollar per share
  - Short-sell securities at price of 100
  - Margin/haircut: $m^{j-}_t=110-100=10$
  - Capital use: \$10 x^{j-}_t
- Positions frequently marked to market
  - payment of $x^j_t(p^j_t-p^j_{t-1})$ plus interest
  - margins potentially adjusted – *more later on this*
- Margins/haircuts must be financed with capital:

$$\sum_j (x^{j+}_t m^{j+}_t + x^{j-}_t m^{j-}_t) \cdot W_t, \text{ where } x^j=x_t^{j+}-x_t^{j-}$$

with perfect cross-margining: $M_t (x_t^1, \ldots, x_t^J) \cdot W_t$

BP: Liquidity Spirals

- Borrowers' balance sheet
  - Loss spiral – net worth drops
    - Net wealth > α x
      for asym. info reasons
    - constant or increasing leverage ratio
  - Margin/haircut spiral
    - Higher margins/haircuts
    - No rollover
    - redemptions
    - forces to delever

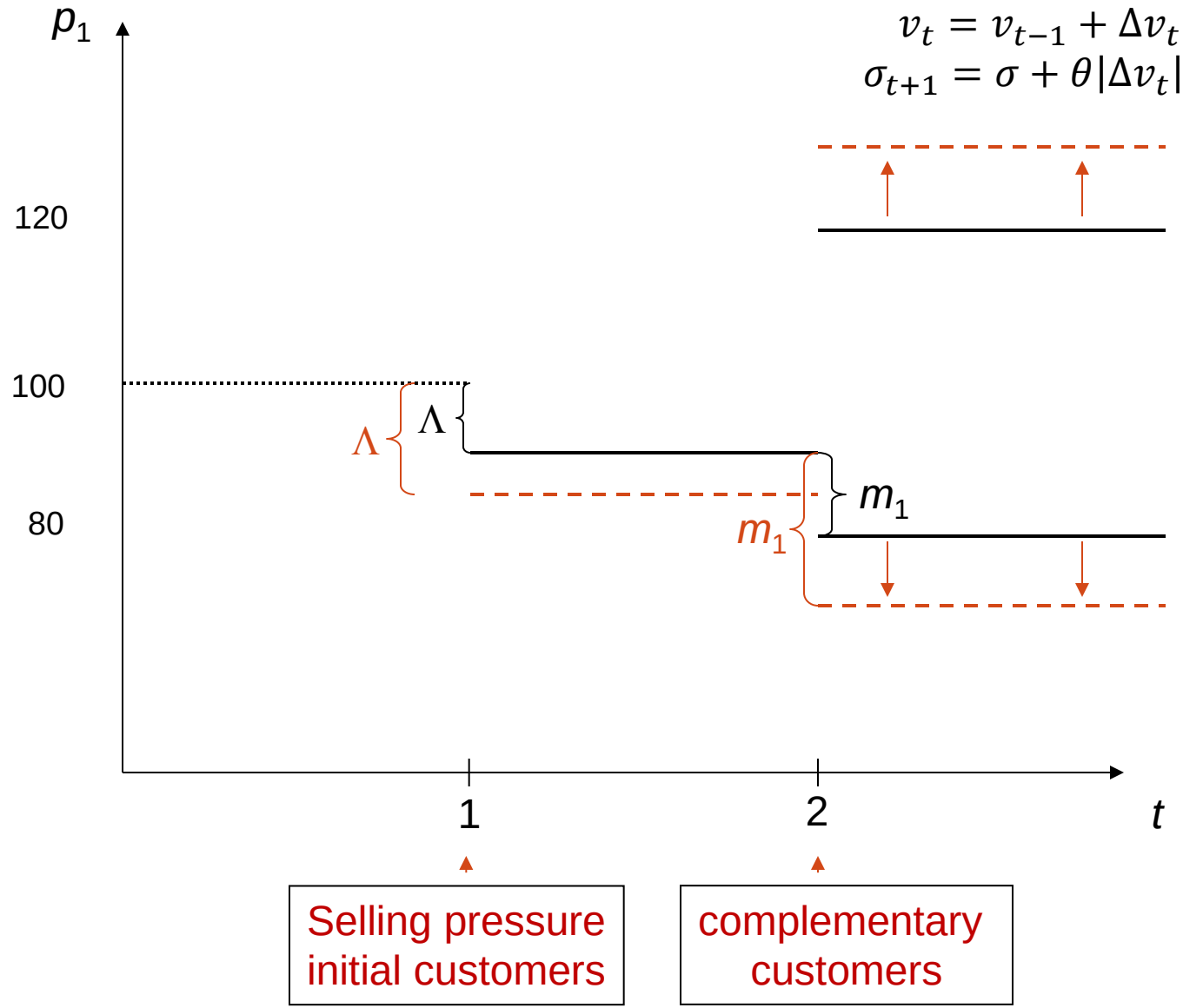


- Mark-to-market vs. mark-to-model
  - worsens loss spiral
  - improves margin spiral

• Both spirals reinforce each other

BP: Margin Spiral – Increased Volatility

$$v_t = v_{t-1} + \Delta v_t = v_{t-1} + \sigma_t \varepsilon_t$$
$$\sigma_{t+1} = \sigma + \theta |\Delta v_t|$$



BP: Margin Spirals - Intuition

1. Volatility of collateral increases
   - Permanent price shock is accompanied by higher future volatility (e.g. ARCH)
     - Realization how difficult it is to value structured products
   - Value-at-Risk shoots up
   - Margins/haircuts increase = collateral value declines
   - Funding liquidity dries up
   - Note: all "expert buyers" are hit at the same time, SV 92
2. Adverse selection of collateral
   - As margins/ABCP rate increase, selection of collateral worsens
   - SIVs sell-off high quality assets first (empirical evidence)
   - Remaining collateral is of worse quality

BP: Model Setup

- Time: t=0,1,2
- Asset with final asset payoff v follows ARCH process
  - $v_t = v_{t-1} + \Delta v_t = v_{t-1} + \sigma_t \varepsilon_t$, where $v_t := E_t[v]$
  - $\sigma_{t+1} = \sigma + \theta |\Delta v_t|$
- Market illiquidity measure: $\Lambda_t = |v_t - p_t|$
- Agents:
  - *Initial customers* with supply $S(z, v_t - p_t)$ at t=1,2
  - *Complementary customers'* demand $D(z, v_2 - p_2)$ at t=2
  - Risk-neutral *dealers* provide *immediacy* and
    - face capital constraint:
      $$xm(\sigma, \Lambda) \leq W(\Lambda) := \max\{0, \underbrace{B}_{\text{cash}} + \underbrace{x_0(E[v_1] - \Lambda)}_{\text{“price” of stock holding}}\}$$
  - *Financiers* set margins

BP: Financiers' Margin Setting

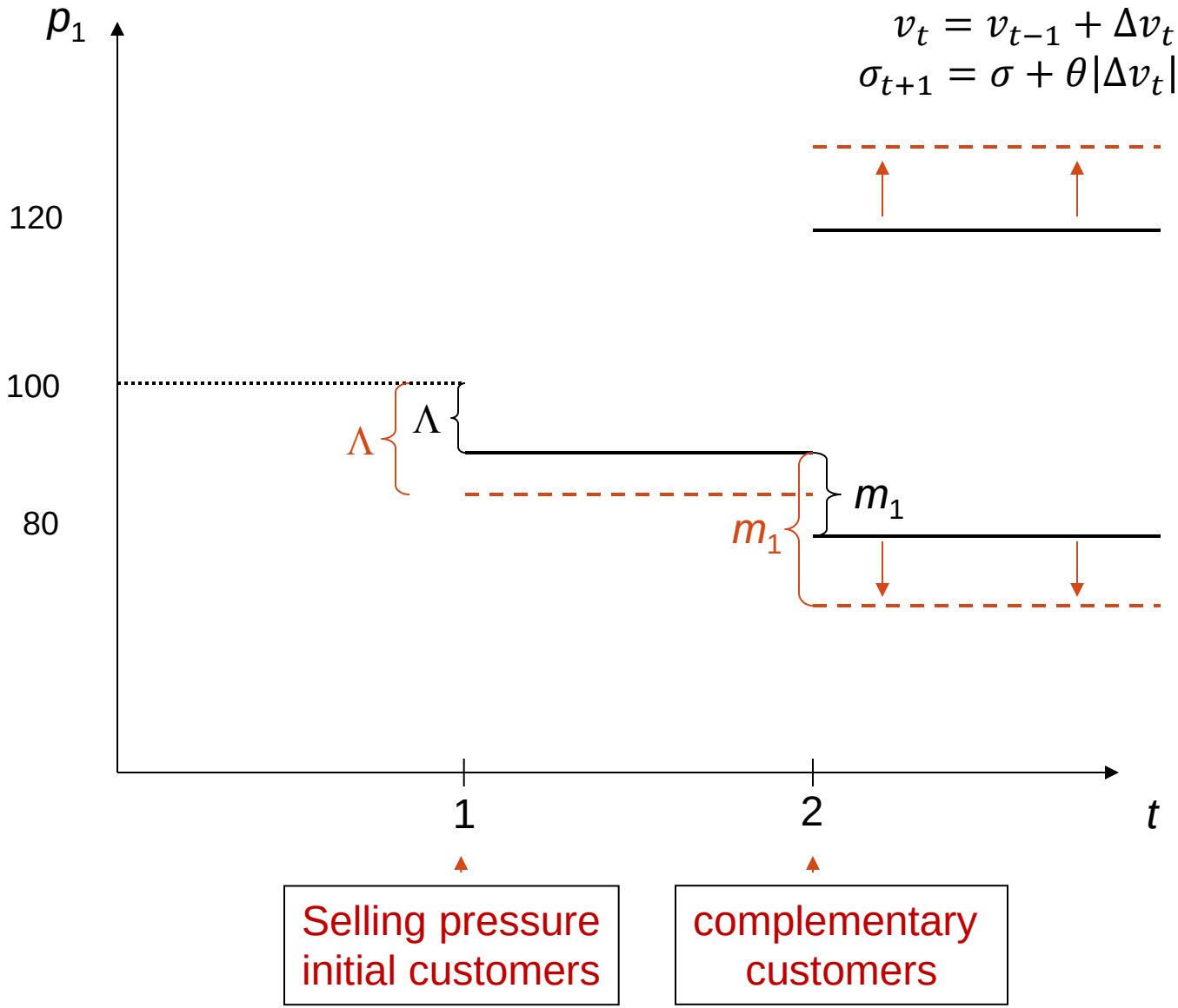
- Margins are set based on Value-at-Risk
- *Financiers* do not know whether price move is due to
  - *Likely*, movement in fundamental (based on ARCH process)
  - *Rare*, Selling/buying pressure by customers who suffered asynchronous endowment shocks.

$$m_1^+ = \underbrace{\Phi^{-1}(1-\pi)}_{\text{CDF}}\sigma_2 = \bar{\sigma} + \bar{\theta}|\Delta p_1| = m_1^-$$

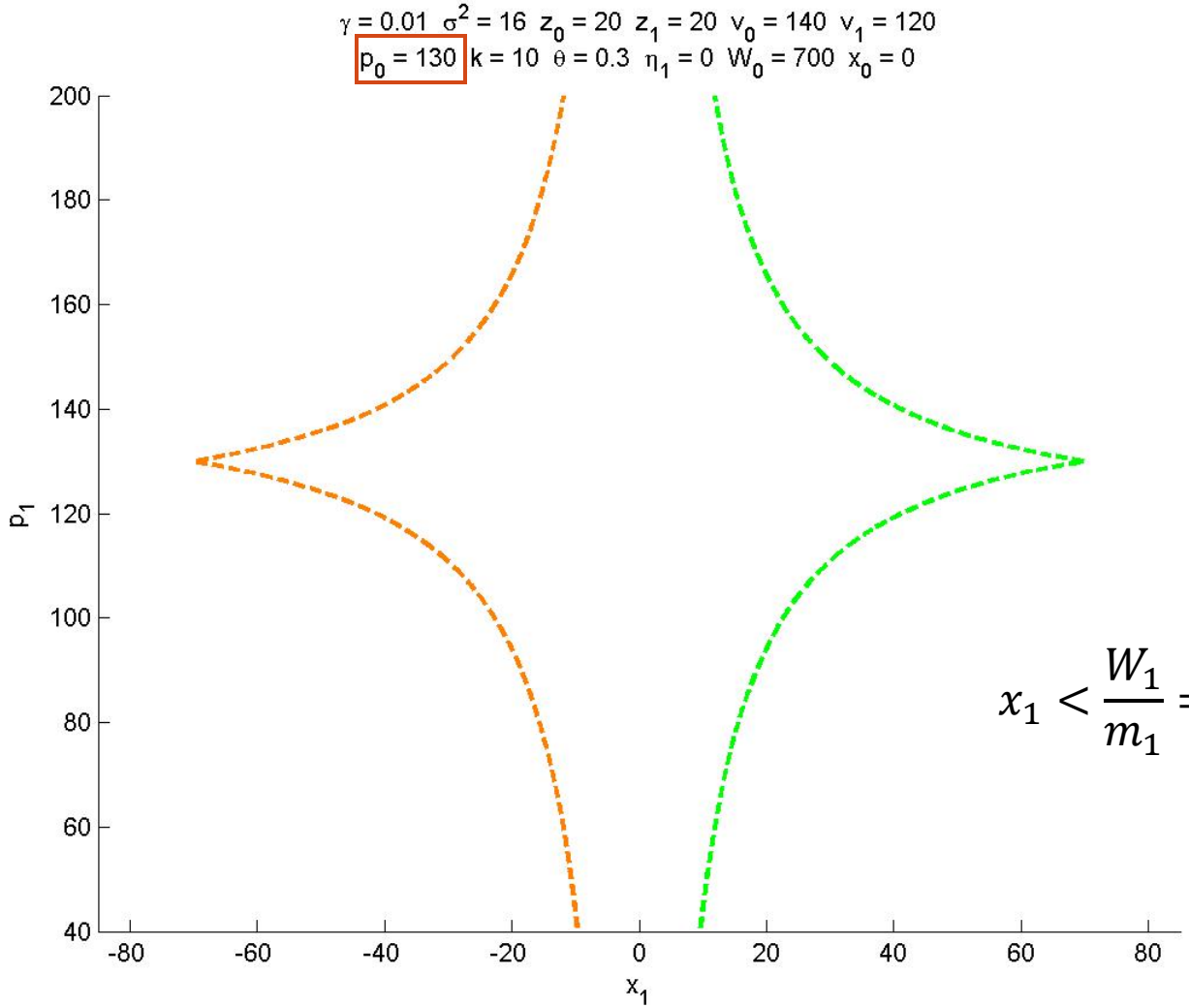
Recall $\sigma_{t+1} = \sigma + \theta|\Delta v_t|$

BP: Margin Spiral – Increased Volatility

$$v_t = v_{t-1} + \Delta v_t = v_{t-1} + \sigma_t \varepsilon_t$$
$$\sigma_{t+1} = \sigma + \theta |\Delta v_t|$$

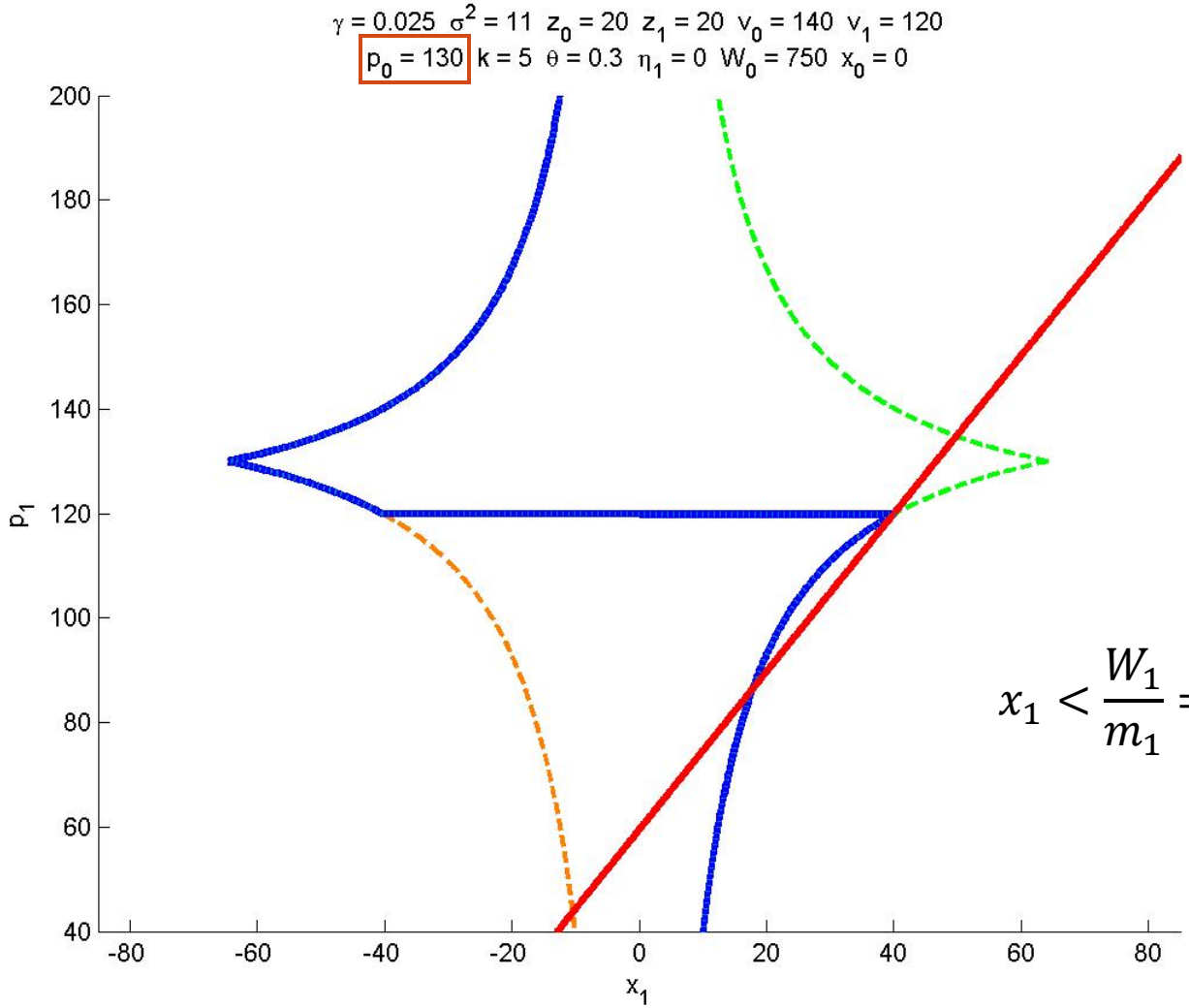


1. Margin Spiral – Increased Volatility



$$x_1 < \frac{W_1}{m_1} = \frac{W_1}{\bar{\sigma} + \bar{\theta}|\Delta p_1|}$$

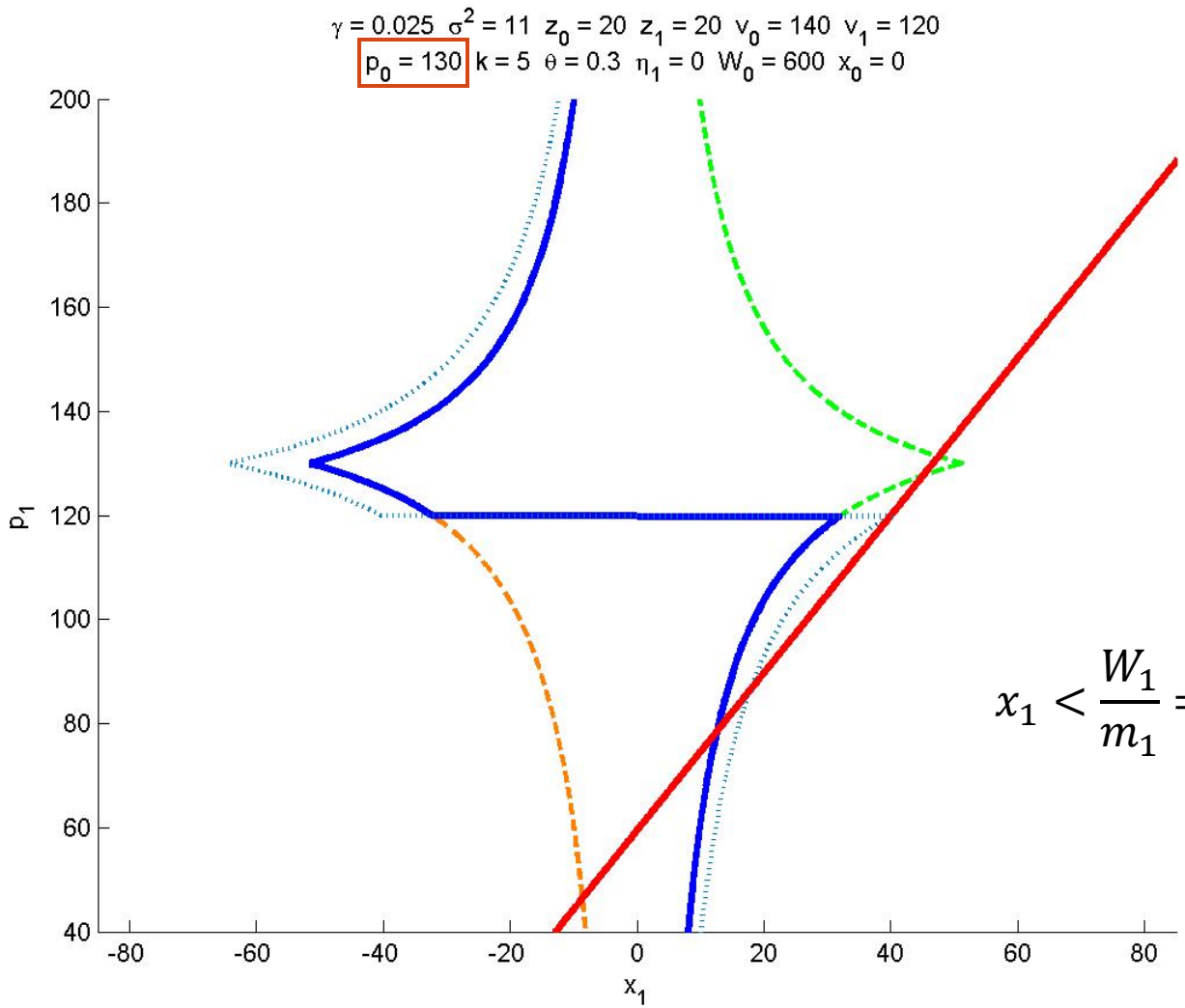
1. Margin Spiral – Increased Volatility



customers' supply

$$x_1 < \frac{W_1}{m_1} = \frac{W_1}{\bar{\sigma} + \bar{\theta}|\Delta p_1|}$$

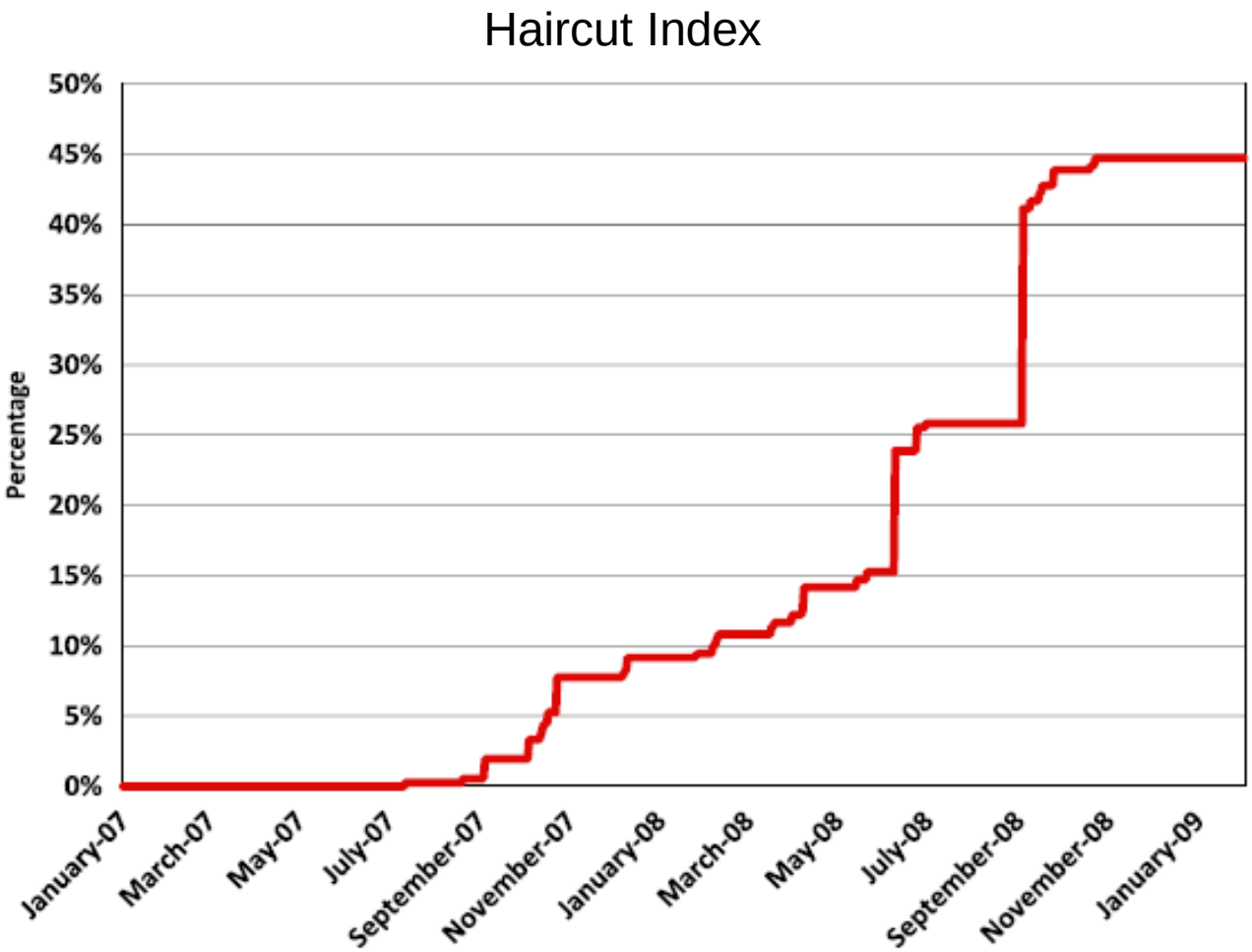
1. Margin Spiral – Increased Volatility



customers' supply

$$x_1 < \frac{W_1}{m_1} = \frac{W_1}{\bar{\sigma} + \bar{\theta}|\Delta p_1|}$$

Data Gorton and Metrick (2011)



"The Run on Repo"

Copeland, Martin, Walker (2011)

Margins **stable** in tri-party repo market

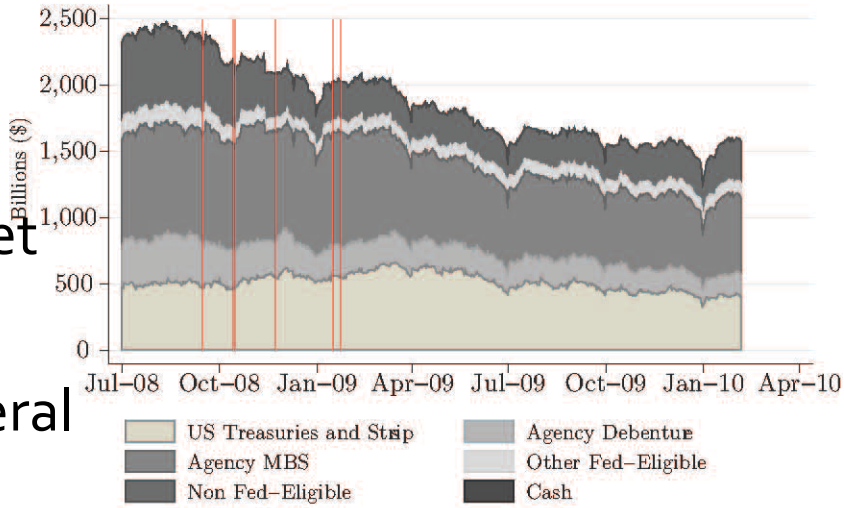
- contrasts Gorton and Metrick
- no general run on certain collateral

Run (non-renewed financing) only on select **counterparties**

- Bear Stearns (anecdotally)
- Lehman (in the data)

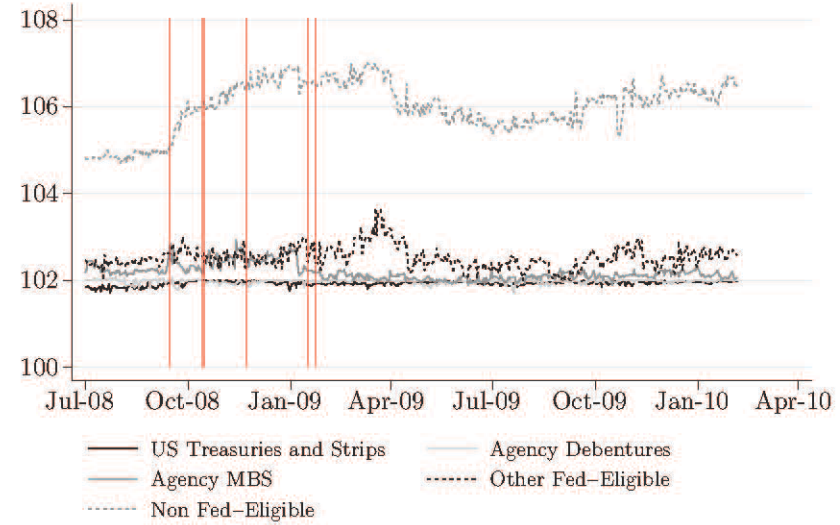
Like 100% haircut…
(**counterparty specific!**)

Figure 6: Stacked Graph of Collateral



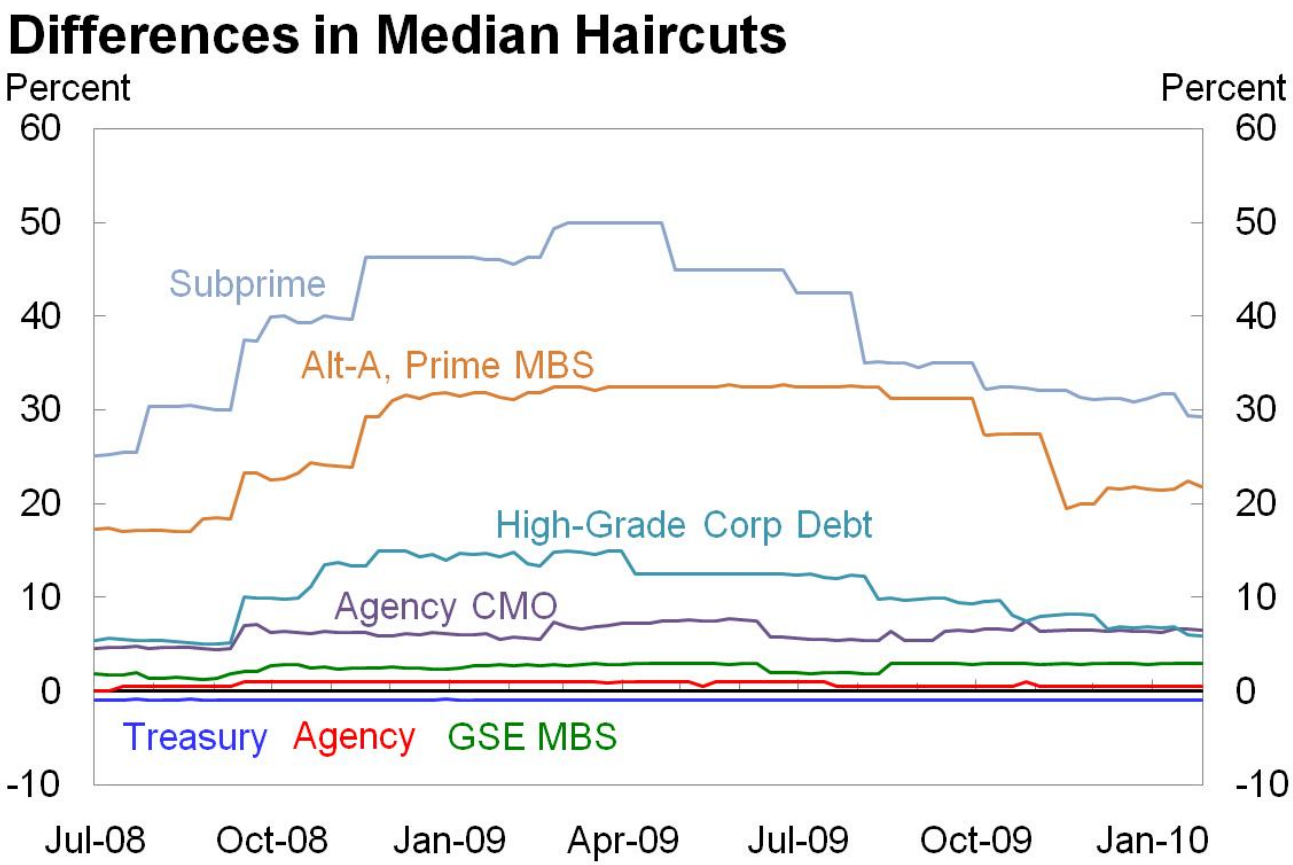
Note: July 17, 2008 excluded because no data was available for BNYM on that date.
Red lines correspond to important market events. From left to right: 9/15/08 (Lehman), 10/14/08 (9 banks receive aid), 10/16/08 (UBS), 11/23/08 (Citi), 1/16/09 (B of A), 1/24/09 (Citi).

Figure 7: Median Haircuts by Asset Type



Note: Red lines correspond to important market events. From left to right: 9/15/08 (Lehman), 10/14/08 (9 banks receive aid), 10/16/08 (UBS), 11/23/08 (Citi), 1/16/09 (B of A), 1/24/09 (Citi).

Bilateral and Tri-party Haircuts?



Source: FRBNY Calculations

BP: Multiple Assets

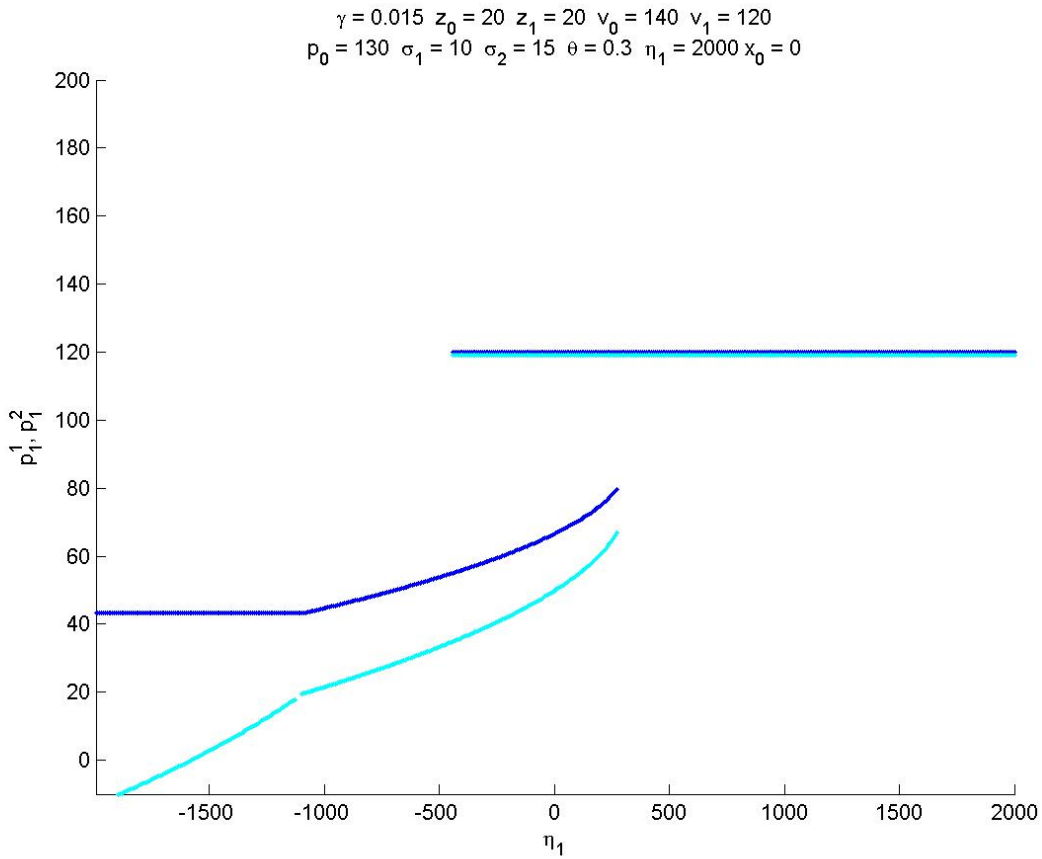
- Dealer maximizes expected profit per capital use
  - Expected profit $E_1[v^j] - p^j = \Lambda^j$
  - Capital use m^j
- Dealers
  - Invest only in securities with highest ratio Λ^j/m^j
- Hence, illiquidity/margin ratio Λ^j/m^j is constant

BP: Commonality & Flight to Quality

- Commonality
  - Since funding liquidity is driving common factor
- Flight to Quality
  - Quality=Liquidity
    Assets with lower fund vol. have better liquidity
  - Flight
    liquidity differential widens when funding liquidity becomes tight

BP: Flight to Quality

m^2=Volatility of Security2 = 2 > 1 = Volatility of Security1=m^1



Macro-literature on Frictions

1. Net worth effects:
   a. Persistence: Carlstrom & Fuerst
   b. Amplification: Bernanke, Gertler & Gilchrist
      "Kocherlakota critique"
2. Volatility effects: impact credit quantity constraints
   a. Instability: Brunnermeier & Sannikov
   b. Margin spirals : Brunnermeier & Pederson
   c. Endogenous constraints: Geanakoplos
3. Demand for liquid assets & Bubbles – "self insurance"
   a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,…
4. Financial intermediaries & Theory of Money