



MACRO, MONEY AND FINANCE

MARKUS BRUNNERMEIER AND YULIY SANNIKOV

Princeton University

■ Motivation

- Aim: Bridge the gap between
 - Macro/monetary research
 - Finance research
- Financial sector helps to
 - overcome financing frictions and
 - channels resources
 - creates money
- ... but
 - Credit crunch due to adverse feedback loops & liquidity spirals
 - Non-linear dynamics
- New insights to monetary and international economics



Output (gap)



■ Price stability
Monetary policy

■ Financial stability
Macroprudential
policy

■ Fiscal debt
sustainability
Fiscal

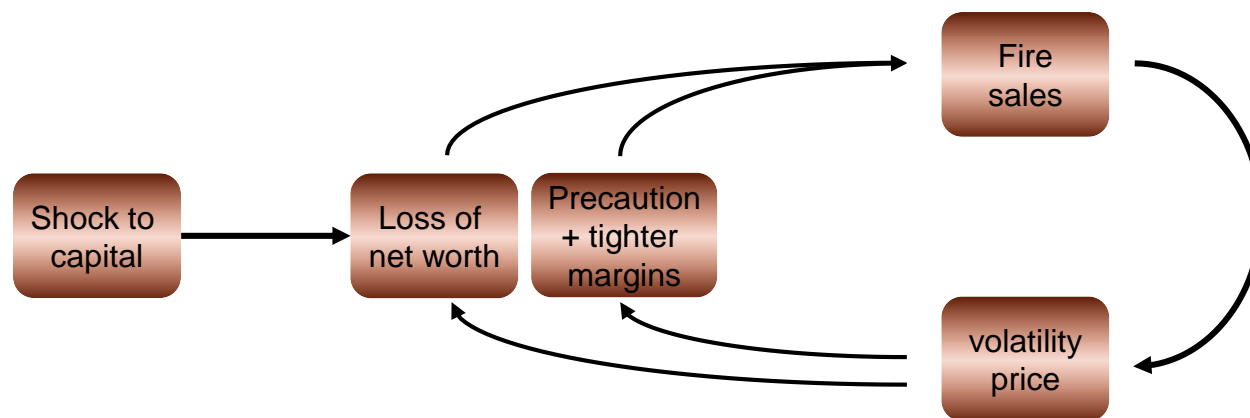
- Short-term interest
- Policy rule (terms structure)
- Reserve requirements
- Capital/liquidity requirements
- Collateral policy
Margins/haircuts
- Capital controls

◀ inter-
action ▶

◀ inter-
action ▶

Systemic risk – a broad definition

- Systemic **risk build-up** during (credit) **bubble** ... and materializes in a crisis
 - “Volatility Paradox” → contemp. measures inappropriate
- Spillovers/contagion – **externalities**
 - Direct contractual: domino effect (interconnectedness)
 - Indirect: price effect (fire-sale externalities)
credit crunch, liquidity spirals



- *Adverse GE response* → **amplification, persistence**

preventive

crisis management

|| Minsky moment – Wile E. Coyote Effect



Methodology – relation to finance

timeline

■ *Verbal Reasoning* (qualitative)

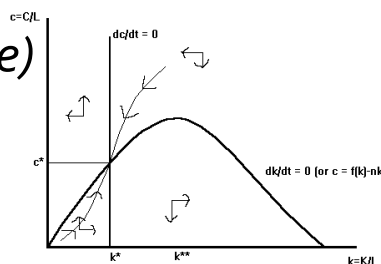
Fisher, Keynes, ...

Macro

Finance

□ Growth theory

- *Dynamic (cts. time)*
- *Deterministic*

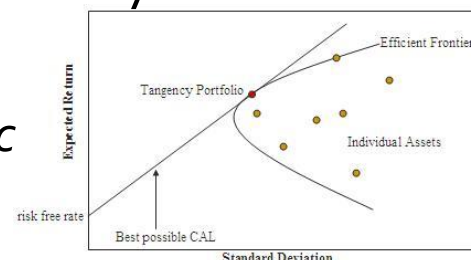


□ Introduce stochastic

- *Discrete time*
 - Brock-Mirman, Stokey-Lucas
 - DSGE models

□ Portfolio theory

- *Static*
- *Stochastic*



□ Introduce dynamics

- *Continuous time*
 - Options Black Scholes
 - Term structure CIR
 - Agency theory Sannikov

■ Cts. time macro with financial frictions

Pre-crisis Macro emphasis

- Price/wage rigidities
- Expectations of
 - cash flow
 - “the” short-term interest rate

Post crisis Macro&Finance

- Financial frictions
- Endogenous risk/volatility
e.g. runs, sudden stops, ...
- Risk premia time varying

$$\Delta \text{price} = f(\Delta E[\text{future cash flows}], \Delta \text{risk premia})$$

- Expectation hypothesis
 - Credit spread = expected default
- Euler equation
 - Substitution effects

- Term risk premia
 - Credit risk premia

- Wealth redistribution
 - Income/wealth effect

*Risk premium news
the main driver*

|| Heterogeneous agents + frictions

- Lending-borrowing/insuring since agents are different

- Poor-rich
- Productive
- Less patient
- Less risk averse
- More optimistic

← Limited direct lending
due to frictions

- Rich-poor
- Less productive
- More patient
- More risk averse
- More pessimistic

- Friction → $p_s MRS_s$ different even after transactions
- **Wealth distribution matters!** (net worth of subgroups)
- Financial sector is not a veil



LIQUIDITY – PERSISTENCE & AMPLIFICATION

MARKUS BRUNNERMEIER AND YULIY SANNIKOV

Princeton University

Liquidity Concepts

- Financial instability arises from the fragility of liquidity

A

L

Technological liquidity

- Reversibility of investment

Market liquidity

- Specificity of capital
Price impact of capital sale

Funding liquidity

- Maturity structure of debt
 - Can't roll over short term debt
- Sensitivity of margins
 - Margin-funding is recalled

~~Liquidity~~
Maturity mismatch

- Liquidity mismatch* determines severity of amplification, (sunspot) runs, ... “strategic complementarities”

Types of Funding Constraints

- Equity constraint

- “Skin in the game constraint”

- + Debt constraints

- Costly state verification a la Townsend

CF, BGG

- Borrowing cost increase as net worth drops

- Collateral/leverage/margin constraints

KM, BP, G

- Quantity constraint on borrowing

- Incomplete contracts a la Hart-Moore

- Commitment problem

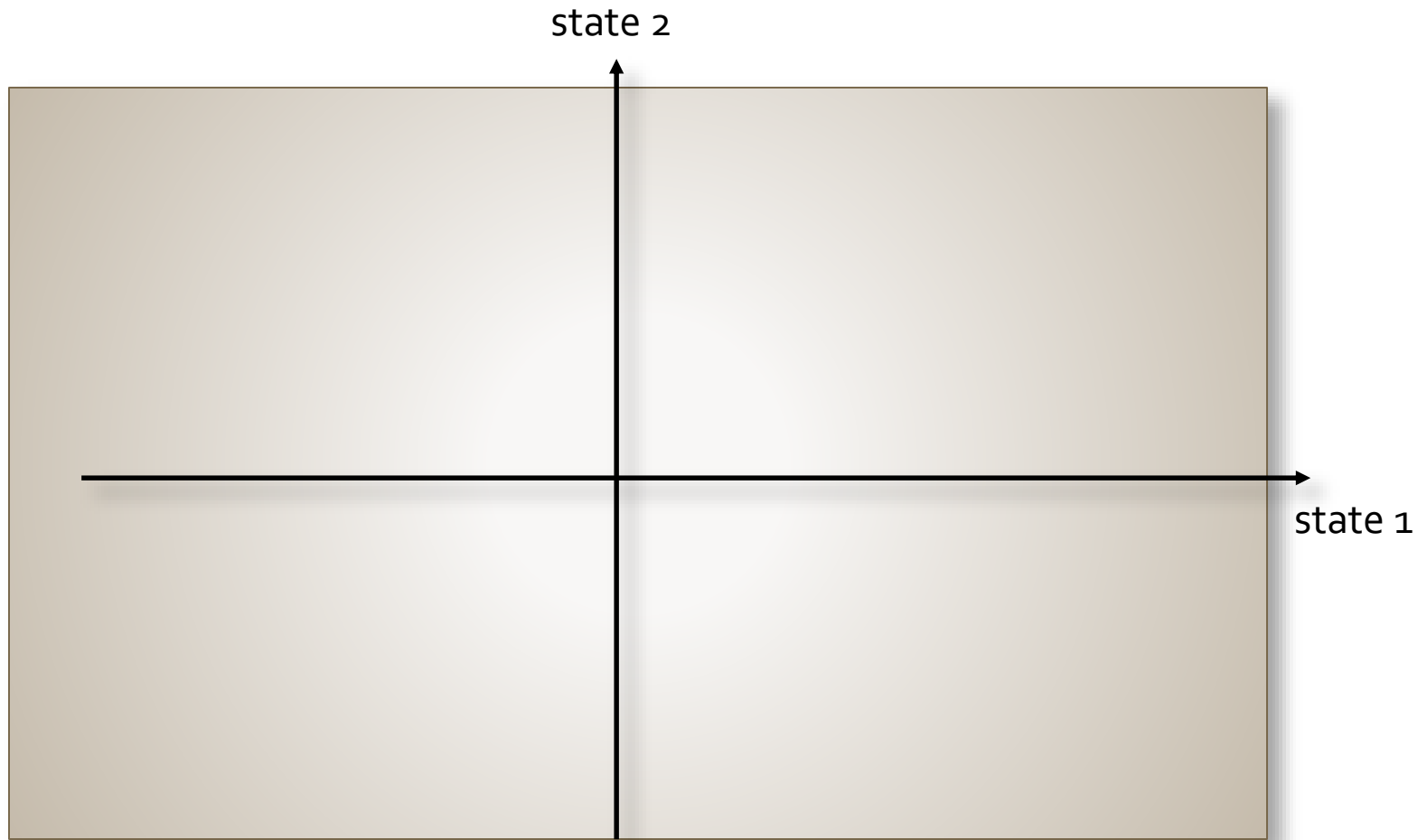
- Credit rationing a la Stiglitz-Weiss

- Not binding (precautionary buffer)

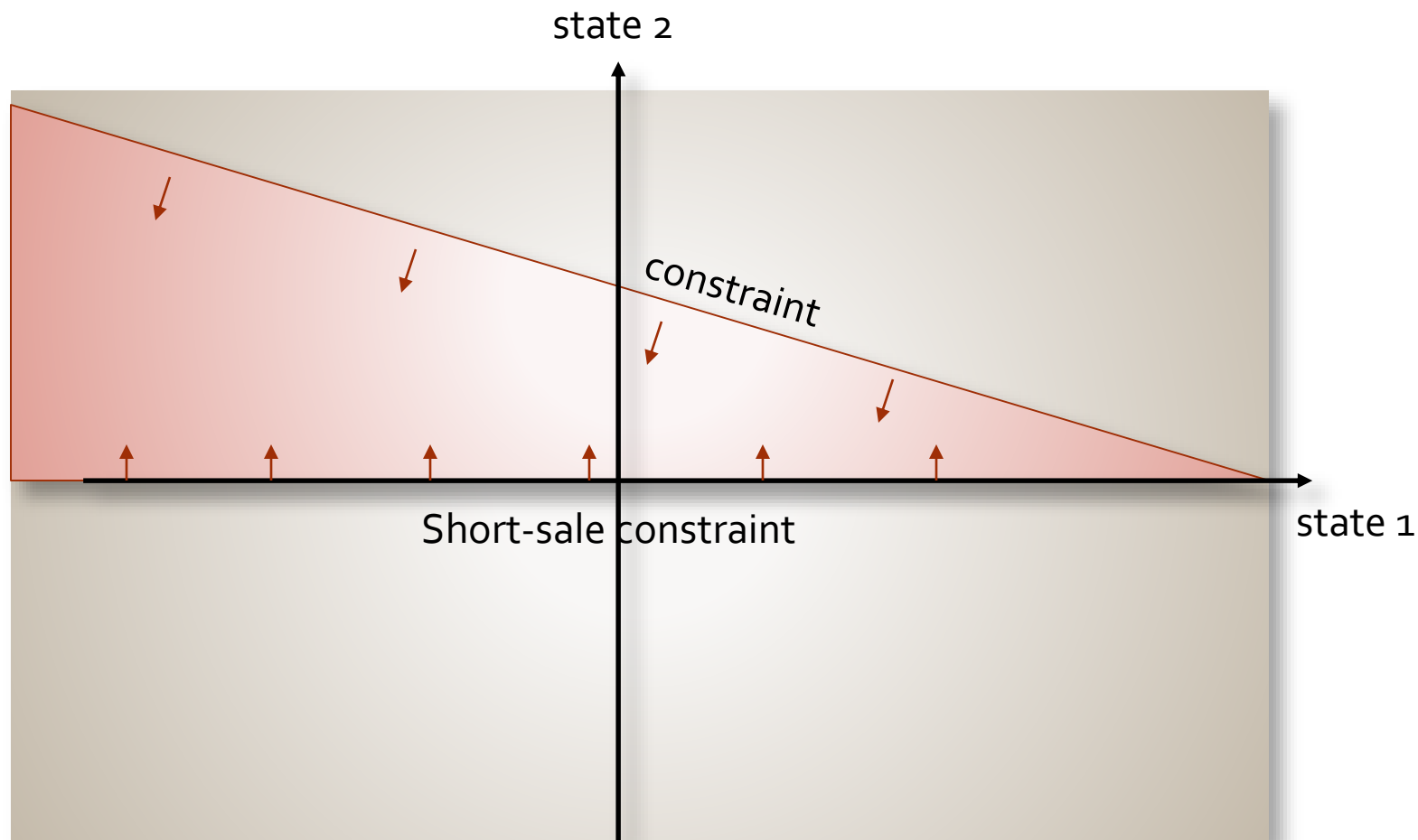
BruSan, He-Krishnamurthy

Comment: Constraints vs. incomplete markets

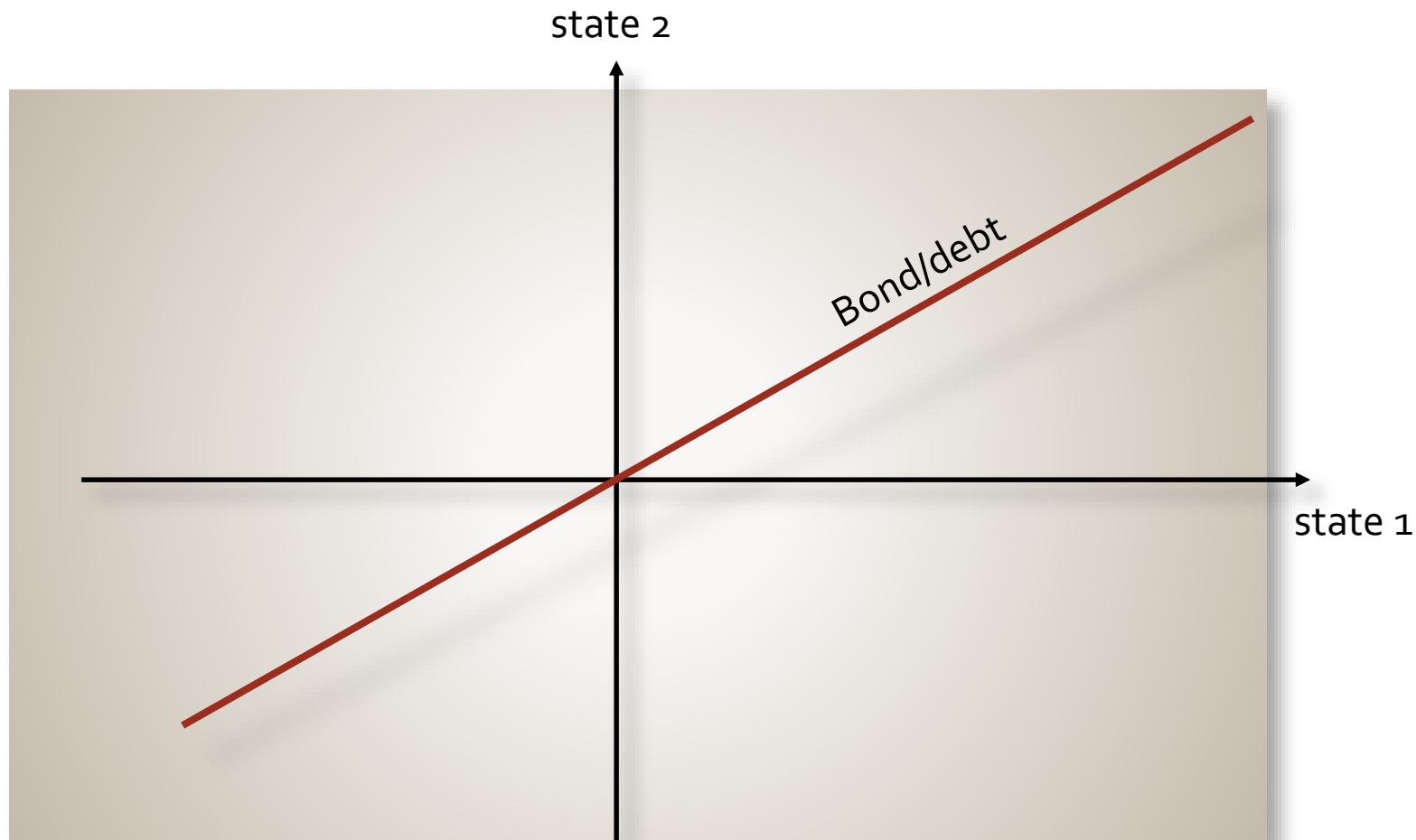
Constraints vs. Incomplete Markets



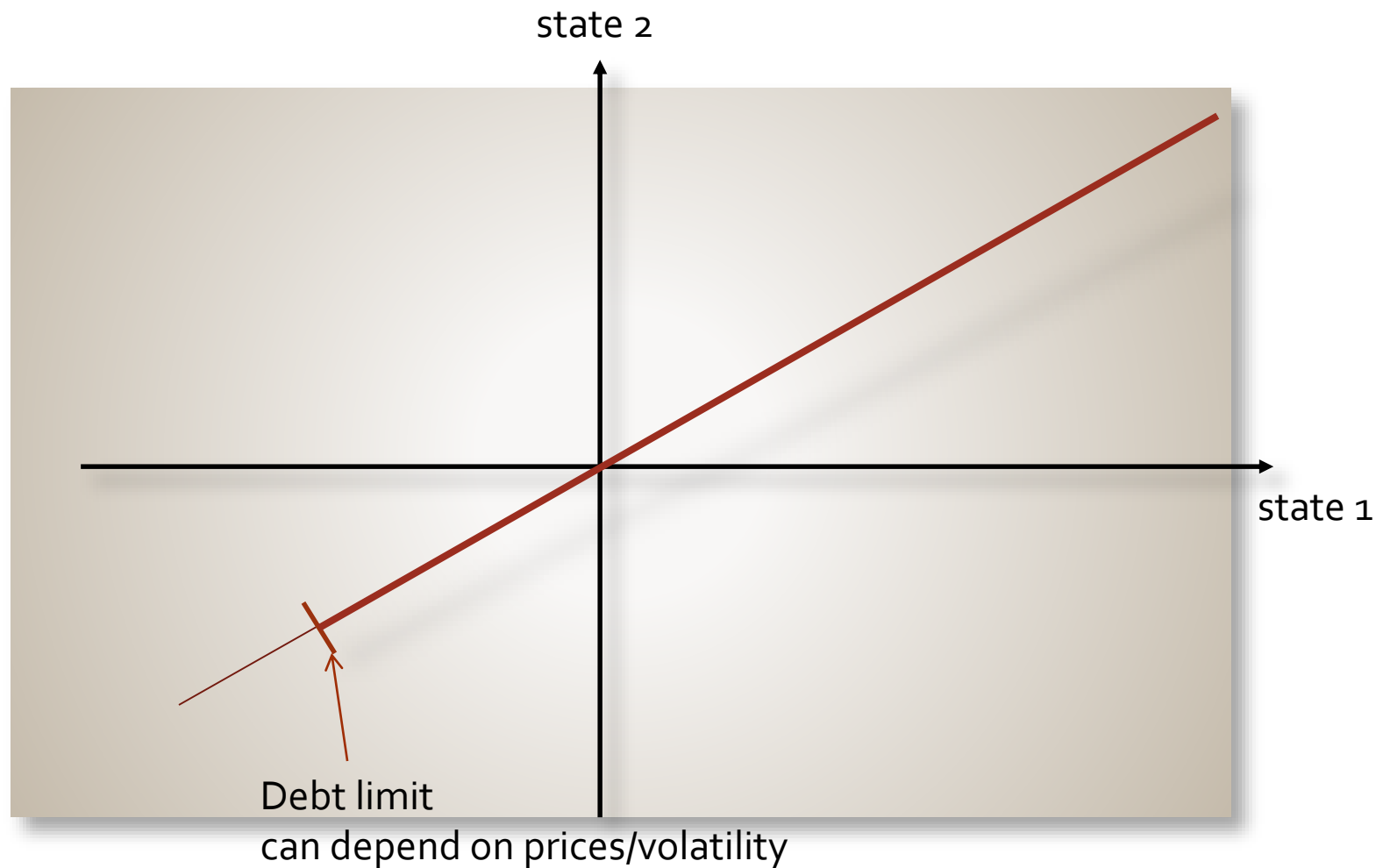
Constraints vs. Incomplete Markets



Constraints vs. Incomplete Markets



Constraints & Incomplete Markets



Amplification vs. inefficiency

- Amplification/ multiplicity:
Strategic complementarities
- Inefficiencies:
externalities

Macro-literature on Frictions

1. Net worth effects:

- a. Persistence: Carlstrom & Fuerst
- b. Amplification: Bernanke, Gertler & Gilchrist
"Kocherlakota critique" & "single shock critique"

2. Volatility effects: impact credit quantity constraints

- a. Instability: Brunnermeier & Sannikov
- b. Margin spirals : Brunnermeier & Pederson
- c. Endogenous constraints: Geanakoplos

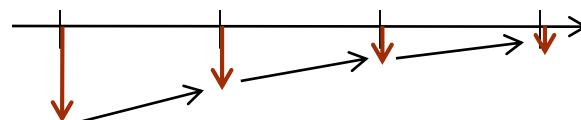
3. Demand for liquid assets & Bubbles – "self insurance"

- a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,...

4. Financial intermediaries & Theory of Money

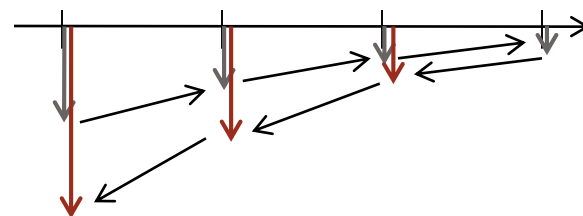
Amplification & Instability - Overview

- Bernanke & Gertler (1989), Carlstrom & Fuerst (1997)
 - Perfect (technological) liquidity, but **persistence**
 - Bad shocks erode net worth, cut back on investments, leading to low productivity & low net worth of in the next period



Amplification & Instability - Overview

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 - Perfect (technological) liquidity, but **persistence**
 - Bad shocks erode net worth, cut back on investments, leading to low productivity & low net worth of in the next period
- Kiyotaki & Moore (1997), BGG (1999)
 - Technological/market illiquidity
 - KM: Leverage bounded by margins; BGG: Verification cost (CSV)
 - Stronger **amplification** effects through **prices** (low net worth reduces leveraged institutions' demand for assets, lowering prices and further depressing net worth)
- Brunnermeier & Sannikov (2010)
 - Instability, volatility dynamics, volatility paradox, Kocherlakota critique
- Brunnermeier & Pedersen (2009), Geanakoplos
 - Volatility interaction with margins/haircuts (leverage)

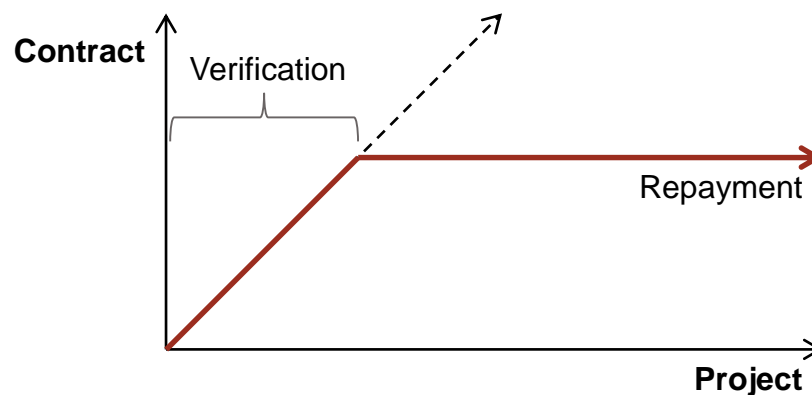


■ Persistence

- Even in standard real business cycle models, temporary adverse shocks can have long-lasting effects
- Due to feedback effects, persistence is much stronger in models with *financial frictions*
 - Bernanke & Gertler (1989)
 - Carlstrom & Fuerst (1997)
- Negative shocks to net worth exacerbate frictions and lead to lower capital, investment and net worth in future periods

Costly State Verification

- Key friction in previous models is costly state verification, i.e. CSV, a la Townsend (1979)
- Borrowers are subject to an idiosyncratic shock
 - Unobservable to lenders, but can be verified at a cost
- Optimal solution is given by a contract that resembles standard debt

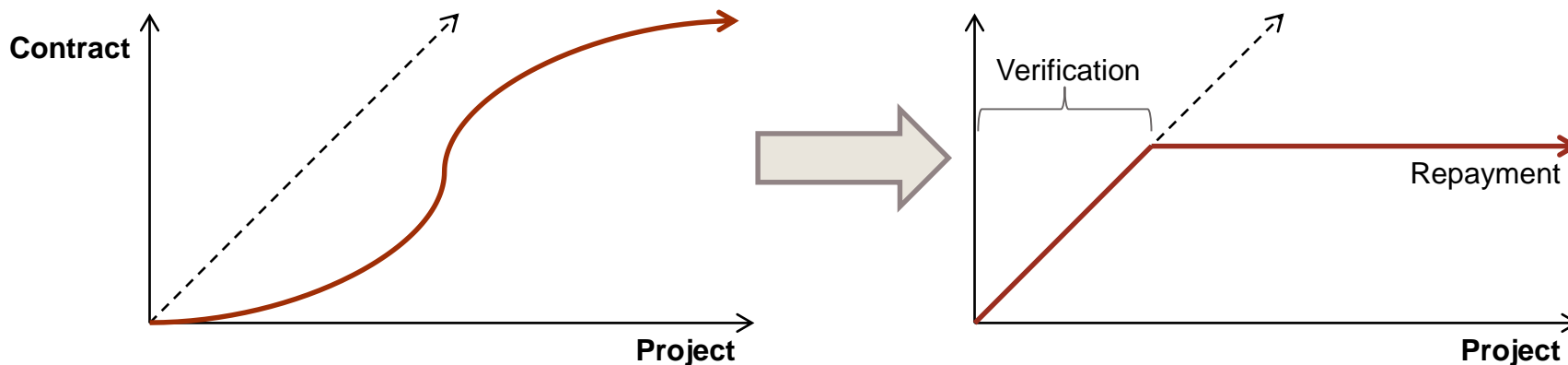


CSV: Contracting

- Competitive market for capital
 - Lender's expected profit is equal to zero
 - Borrower's optimization is equivalent to minimizing expected verification cost
- Financial contract specifies:
 - Debt repayment for each reported outcome
 - Reported outcomes that should be verified

CSV: Optimal Contract

- Incentive compatibility implies that
 - Repayment outside of VR is constant
 - Repayment outside of VR is weakly greater than inside
- Maximizing repayment in VR reduces the size and thus the expected verification cost



■ Carlstrom & Fuerst

- Output is produced according to $Y_t = A_t f(K_t)$
- Fraction η of entrepreneurs and $1 - \eta$ of households
 - Only entrepreneurs can create new capital from consumption goods
- Individual investment yields ωi_t of capital
 - Shock is given by $\omega \sim G$ with $E[\omega] = 1$
 - This implies consumption goods are converted to capital one-to-one in the *aggregate*
 - *No technological illiquidity!*

CF: Costly State Verification

- Households can verify ω at cost μi_t
 - Optimal contract is debt with audit threshold $\bar{\omega}$
 - Entrepreneur with net worth n_t borrows $i_t - n_t$ and repays $\min\{\omega_t, \bar{\omega}\} \times i_t$
- Auditing threshold is set by HH breakeven condition
 - $$\left[\int_0^{\bar{\omega}} (\omega - \mu) dg(\omega) + (1 - G(\bar{\omega}))\bar{\omega} \right] i_t q_t = i_t - n_t$$
 - Here, q_t is the price of capital
- No positive interest (within period borrowing) and no risk premium (no aggregate investment risk)

CF: Persistence & Dampening

- Negative shock in period t decreases N_t
 - This increases financial friction and decreases I_t
- Decrease in capital supply leads to
 - Lower capital: K_{t+1}
 - Lower output: Y_{t+1}
 - Lower net worth: N_{t+1}
 - Feedback effects in future periods $t + 2, \dots$
- Decrease in capital supply also leads to
 - Increased price of capital q_t
 - Dampening effect on propagation of net worth shock

Dynamic Amplification

- Bernanke, Gertler and Gilchrist (1999) introduce *technological illiquidity* in the form of nonlinear adjustment costs to capital
- Negative shock in period t decreases N_t
 - This increases financial friction and decreases I_t
- In contrast to the dampening mechanism present in CF, now decrease in capital demand (not supply) leads to
 - Decreased price of capital due to adjustment costs
 - *Amplification* effect on propagation of net worth shock

■ Bernanke, Gertler & Gilchrist

- BGG assume separate investment sector
 - This separates entrepreneurs' capital decisions from adjustment costs
- $\Phi(\cdot)$ represents *technological illiquidity*
 - Increasing and concave with $\Phi(0) = 0$
 - $K_{t+1} = \Phi\left(\frac{I_t}{K_t}\right) K_t + (1 - \delta)K_t$
- FOC of investment sector
 - $\max_{I_t} \{q_t K_{t+1} - I_t\} \Rightarrow q_t = \Phi'\left(\frac{I_t}{K_t}\right)^{-1}$

[jump to KM97](#)

|| BGG: Entrepreneurs

- Entrepreneurs alone can hold capital used in production (of consumption good)
- At time t , entrepreneurs purchase capital for $t + 1$
 - To purchase k_{t+1} , an entrepreneur borrows $q_t k_{t+1} - n_t$
 - Here, n_t represents entrepreneur net worth
- Assume gross return to capital is given by ωR_{t+1}^k
 - Here $\omega \sim G$ with $E[\omega] = 1$ and ω i.i.d.
 - R_{t+1}^k is the endogenous aggregate equilibrium return

|| BGG: Persistence & Amplification

- Shocks to net worth N_t are persistent
 - They affect capital holdings, and thus N_{t+1}, \dots
- *Technological illiquidity* for capital “demanders” now introduces amplification effect
 - Decrease in capital leads to reduced price of capital from
$$q_t = \Phi' \left(\frac{I_t}{K_t} \right)^{-1}$$
 - Lower price of capital further decreases net worth

■ Kiyotaki & Moore 97

- Kiyotaki, Moore (1997) adopt a
 - collateral constraint instead of CSV
 - *market illiquidity* – second best use of capital
- Output is produced in two sectors, differ in productivity
- Aggregate capital is fixed, resulting in extreme *technological illiquidity*
 - Investment is completely irreversible
- Durable asset has two roles:
 - Collateral for borrowing
 - Input for production

■ KM: Amplification

- *Static* amplification occurs because fire-sales of capital from productive sector to less productive sector depress asset prices
 - Importance of *market liquidity* of physical capital
- *Dynamic* amplification occurs because a temporary shock translates into a persistent decline in output and asset prices

■ KM: Agents

- Two types of infinitely-lived risk neutral agents
- Mass η of productive agents
 - Constant-returns-to-scale production technology yielding $y_{t+1} = ak_t$
 - Discount factor $\beta < 1$
- Mass $1 - \eta$ of less productive agents
 - Decreasing-returns-to-scale production $y_{t+1} = F(k_t)$
 - Discount factor $\underline{\beta} \in (\beta, 1)$
 - Note: Now, we have two different production functions!

■ KM: Frictions

- Since productive agents are less patient, they will want to borrow b_t from less productive agents
 - However, friction arises in that each productive agent's technology requires *his* individual human capital
 - Productive agents cannot pre-commit human capital
- This results in a collateral constraint
$$Rb_t \leq q_{t+1}k_t$$
 - Productive agent will never repay more than the value of his asset holdings, i.e. collateral

■ KM: Demand for Assets

- Since there is no uncertainty, a *productive agent* will borrow the maximum quantity and will not consume any of the output
 - Budget constraint: $q_t k_t - b_t \leq (a + q_t)k_{t-1} - Rb_{t-1}$
 - Demand for assets: $k_t = \frac{1}{q_t - \frac{q_{t+1}}{R}} [(a + q_t)k_{t-1} - Rb_{t-1}]$
- Unproductive agents are not borrowing constrained
 - $R = \underline{\beta}^{-1}$ and asset demand is set by equating margins
 - Demand for assets: $R = \frac{F'(\underline{k}_t) + q_{t+1}}{q_t}$

$$\text{Rewritten to } \frac{1}{R} F'(\underline{k}_t) = q_t - \frac{1}{R} q_{t+1}$$

■ KM: Equilibrium

- With fixed supply of capital, market clearing requires $\eta K_t + (1 - \eta) \underline{K}_t = \bar{K}$
 - This implies $M(K_t) \equiv \frac{1}{R} \underline{F}'\left(\frac{\bar{K} - \eta K_t}{1 - \eta}\right) = q_t - \frac{1}{R} q_{t+1}$
 - Note that $M(\cdot)$ is increasing
- Iterating forward, we obtain: $q_t = \sum_{s=0}^{\infty} \frac{1}{R^s} M(K_{t+s})$

■ KM: Steady State

- In steady state, productive agents use tradable output a to pay interest on borrowing:
- This implies that steady state price q^* must satisfy:
 - $q^* - \frac{1}{R} q^* = a$
- Further, steady state capital K^* must satisfy:
 - $\frac{1}{R} F' \left(\frac{\bar{K} - \eta K^*}{1 - \eta} \right) = a$
 - This reflects inefficiency since marginal products correspond only to *tradable* output as opposed to total $a + c$, where c is non-tradable fraction

■ KM: Productivity Shock

- Log-linearized deviations around steady state:
 - Unexpected one-time shock that reduces production of all agents by factor $1 - \Delta$
- %-change in assets for given change in asset price:
 - $\hat{K}_t = -\frac{\xi}{1+\xi} \left(\Delta + \frac{R}{R-1} \hat{q}_t \right), \hat{K}_{t+s} = \frac{\xi}{1+\xi} \hat{K}_{t+s-1}$
 - $\frac{1}{\xi} = \frac{d \log M(K)}{d \log K} \big|_{K=K^*}$ (elasticity)
- Reduction in assets comes from two shocks:
 - Lost output Δ
 - Capital losses on previous assets $\frac{R}{R-1} \hat{q}_t$, amplified by leverage
 - $\frac{\xi}{1+\xi}$ terms dampens effect since asset can reallocated

■ KM: Productivity Shock

- Change in price for given change in assets:
 - Log-linearize the equation $q_t = \sum_{s=0}^{\infty} \frac{1}{R^s} M(K_{t+s})$
 - This provides: $\hat{q}_t = \frac{1}{\xi} \frac{R-1}{R} \sum_{s=0}^{\infty} \frac{1}{R^s} \hat{K}_{t+s}$
- Combining equations:

Multiplier	static	dynamic
$\hat{K}_t =$	$-\Delta$	$-\frac{1}{(\xi + 1)(R - 1)} \Delta$
$\hat{q}_t =$	$-\frac{(R - 1)}{R} \frac{1}{\xi} \Delta$	$-\frac{1}{R} \frac{1}{\xi} \Delta$

- Static effect results from assuming $q_{t+1} = q^*$

■ “Kocherlakota critique”

- Amplification for negative shocks differs from positive shocks
 - In Kocherlakota (2000) optimal scale of production (positive shock does not lead to expansion)
- Amplification is quantitatively too small
 - Capital share is only $1/3$ and hence GDP is too small
 - Cordoba and Ripoll (2004)
 - Needs sizeable capital share plus
 - Low intertemporal substitution

■ “Single Shock Critique”

- Critique: After the shock all agents in the economy know that the economy will deterministically return to the steady state.
 - Length of slump is deterministic (and commonly known)
 - No safety cushion needed
 - In reality an adverse shock may be followed by additional adverse shocks
 - Build-up extra safety cushion for an additional shock in a crisis

Macro-literature on Frictions

1. Net worth effects:

- a. Persistence: Carlstrom & Fuerst
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"Kocherlakota critique"

2. Volatility effects: impact credit quantity constraints

- a. Instability: Brunnermeier & Sannikov
- b. Margin spirals : Brunnermeier & Pederson
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3. Demand for liquid assets & Bubbles – "self insurance"

- a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,...

4. Financial intermediaries & Theory of Money

|| BruSan14: Instability & Non-Linear Effects

- Previous papers only considered log-linearized solutions around steady state
- Brunnermeier & Sannikov (2014) build a continuous time model to study full dynamics
 - Show that financial system exhibits inherent instability due to highly non-linear effects
 - These effects are asymmetric and only arise in downturn
 - A shock can be followed by future shocks
 - Length of slump is uncertain
- Agents choose a *capital cushion*
 - Mitigates moderate shocks near steady state
 - High volatility away from steady state

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4. Financial intermediaries & Theory of Money

■ Credit Rationing – Quantity Rationing

- Credit rationing refers to a failure of market clearing in credit
 - In particular, an excess demand for credit that fails to increase market interest rate
 - Pool of loan applicants worsens
 - Stiglitz & Weiss (1981) show how asymmetric information on risk can lead to credit rationing

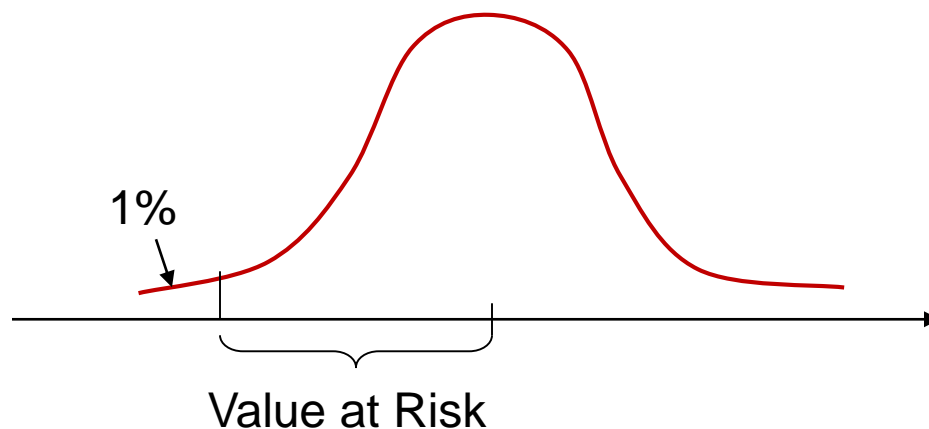
|| Brunnermeier-Pedersen: Margin Spiral

- For collateralized lending, debt constraints are directly linked to the **volatility of collateral**
 - Constraints are more binding in volatile environments
 - **Feedback effect** between **volatility and constraints**
- These margin spirals force agents to delever in times of crisis
 - Collateral runs
 - Multiple equilibria

counterparty bank run

BP: Margins—Value at Risk (VaR)

- How are margins set by brokers/exchanges?
 - **Value at Risk:** $\Pr(-(p_{t+1} - p_t) \geq m) = 1\% = \pi$





BP: Leverage and Margins

- Financing a *long position* of $x_t^{j+} > 0$ shares at price $p_t^j = 100$:
 - Borrow \$90\$ dollar per share;
 - Margin/haircut: $m_t^{j+} = 100 - 90 = 10$
 - Capital use: $\$10 x_t^{j+}$
- Financing a *short position* of $x_t^{j-} > 0$ shares:
 - Borrow securities, and lend collateral of 110 dollar per share
 - Short-sell securities at price of 100
 - Margin/haircut: $m_t^{j-} = 110 - 100 = 10$
 - Capital use: $\$10 x_t^{j-}$
- Positions frequently marked to market
 - payment of $x_t^j (p_t^j - p_{t-1}^j)$ plus interest
 - margins potentially adjusted – *more later on this*
- Margins/haircuts must be financed with capital:

$$\sum_j (x_t^{j+} m_t^{j+} + x_t^{j-} m_t^{j-}) \leq W_t, \text{ where } x_t^j = x_t^{j+} - x_t^{j-}$$

with perfect cross-margining: $M_t(x_t^1, \dots, x_t^J) \leq W_t$

BP: Liquidity Spirals

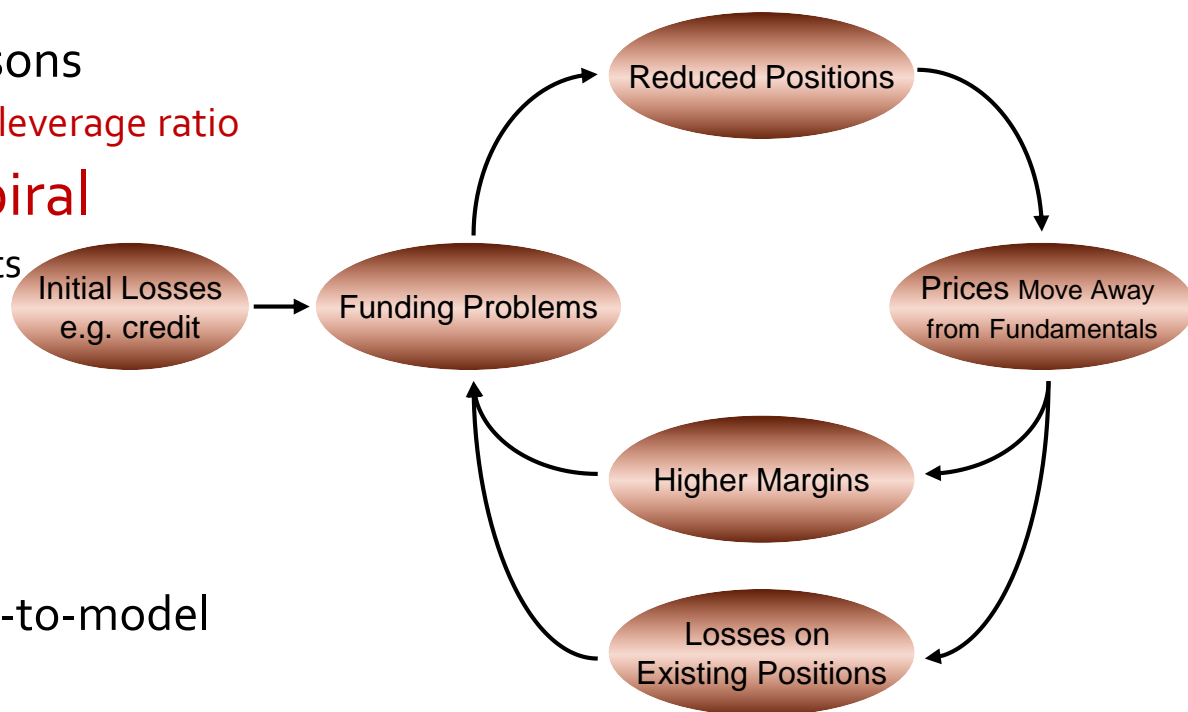
■ Borrowers' balance sheet

▫ Loss spiral – net worth drops

- Net wealth $> \alpha \times$
for asym. info reasons
- constant or increasing leverage ratio

▫ Margin/haircut spiral

- Higher margins/haircuts
- No rollover
- redemptions
- forces to delever

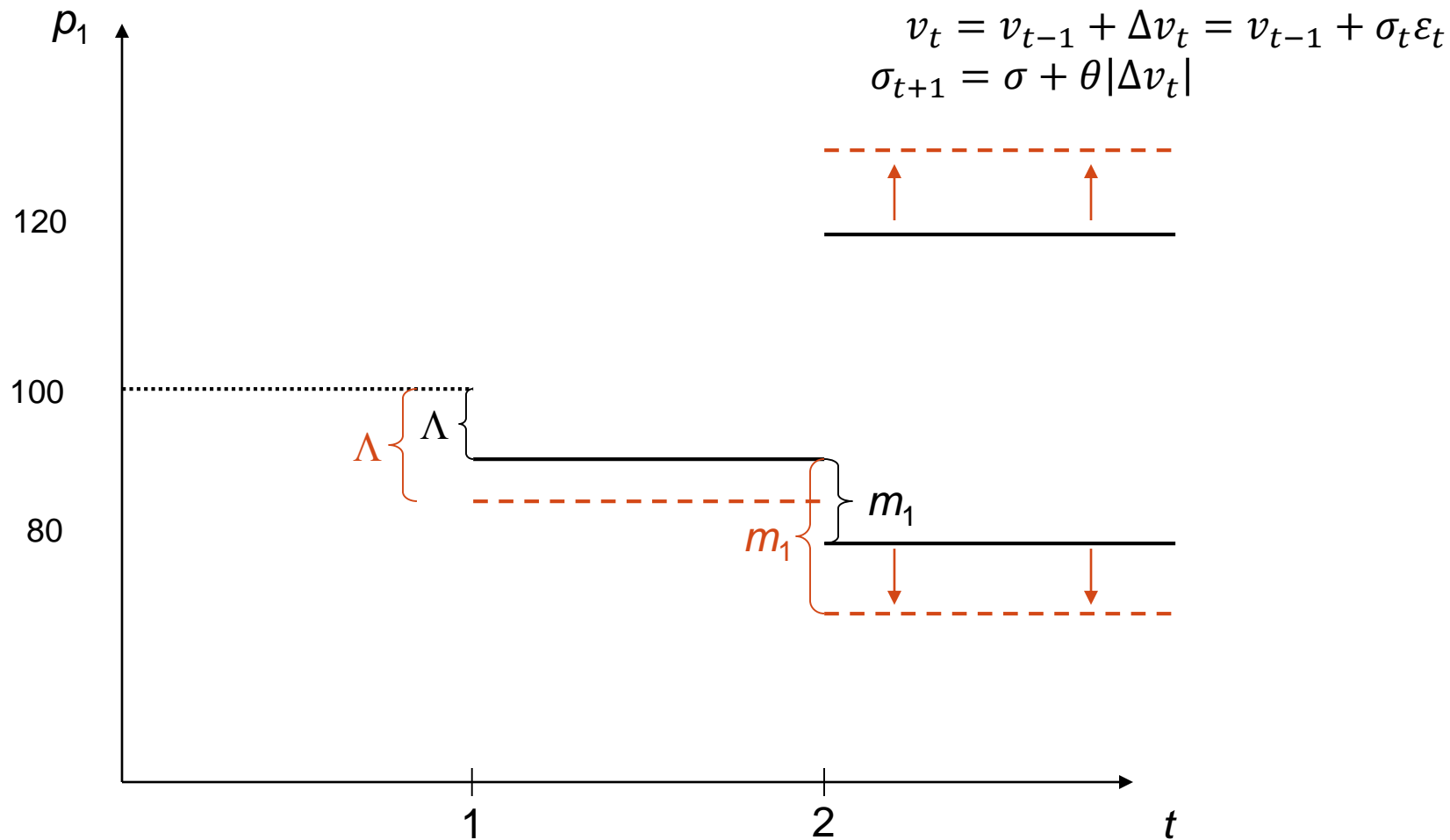


■ Mark-to-market vs. mark-to-model

- worsens loss spiral
- improves margin spiral

• Both spirals reinforce each other

BP: Margin Spiral – Increased Volatility



$$v_t = v_{t-1} + \Delta v_t = v_{t-1} + \sigma_t \varepsilon_t$$

$$\sigma_{t+1} = \sigma + \theta |\Delta v_t|$$

Selling pressure
initial customers

complementary
customers

BP: Margin Spirals - Intuition

1. Volatility of collateral increases

- Permanent price shock is accompanied by higher future volatility (e.g. ARCH)
 - Realization how difficult it is to value structured products
- Value-at-Risk shoots up
- Margins/haircuts increase = collateral value declines
- Funding liquidity dries up
- Note: all “expert buyers” are hit at the same time, SV 92

2. Adverse selection of collateral

- As margins/ABCP rate increase, selection of collateral worsens
- SIVs sell-off high quality assets first (empirical evidence)
- Remaining collateral is of worse quality

BP: Model Setup

- Time: $t=0,1,2$
- Asset with final asset payoff v follows ARCH process
 - $v_t = v_{t-1} + \Delta v_t = v_{t-1} + \sigma_t \varepsilon_t$, where $v_t := E_t[v]$
 - $\sigma_{t+1} = \sigma + \theta |\Delta v_t|$
- Market illiquidity measure: $\Lambda_t = |v_t - p_t|$
- Agents:
 - *Initial customers* with supply $S(z, v_t - p_t)$ at $t=1,2$
 - *Complementary customers'* demand $D(z, v_2 - p_2)$ at $t=2$
 - Risk-neutral *dealers* provide *immediacy* and
 - face capital constraint:

$$xm(\sigma, \Lambda) \leq W(\Lambda) := \max\{0, \underbrace{B}_{\text{cash}} + \underbrace{x_0(E[v_1] - \Lambda)}_{\text{"price" of stock holding}}\}$$
 - *Financiers* set margins



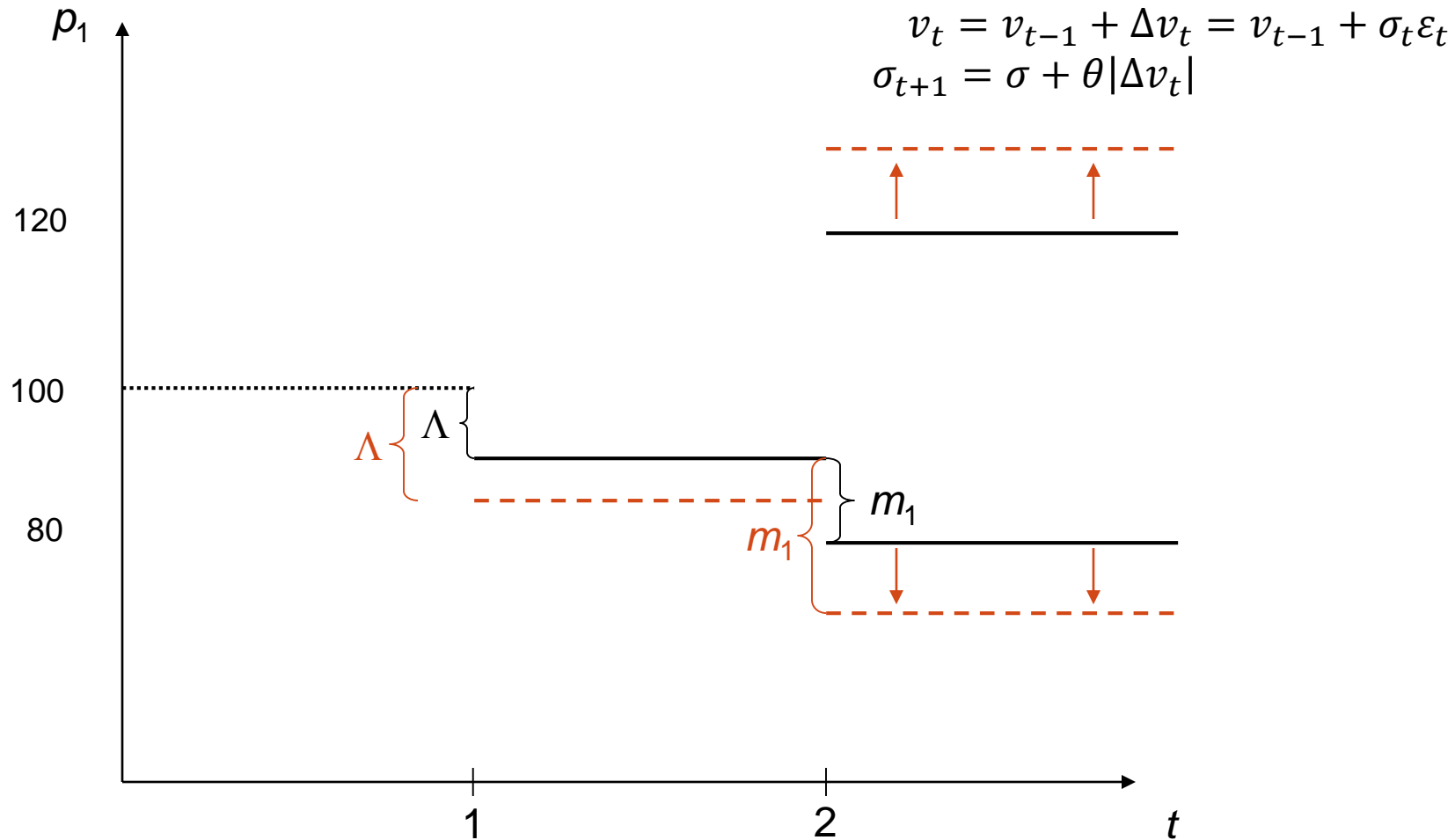
BP: Financiers' Margin Setting

- Margins are set based on Value-at-Risk
- *Financiers* do not know whether price move is due to
 - *Likely*, movement in fundamental (based on ARCH process)
 - *Rare*, Selling/buying pressure by customers who suffered asynchronous endowment shocks.

$$m_1^+ = \underbrace{\Phi^{-1}(1 - \pi)}_{\text{CDF}} \sigma_2 = \bar{\sigma} + \bar{\theta} |\Delta p_1| = m_1^-$$

Recall $\sigma_{t+1} = \sigma + \theta |\Delta v_t|$

BP: Margin Spiral – Increased Volatility



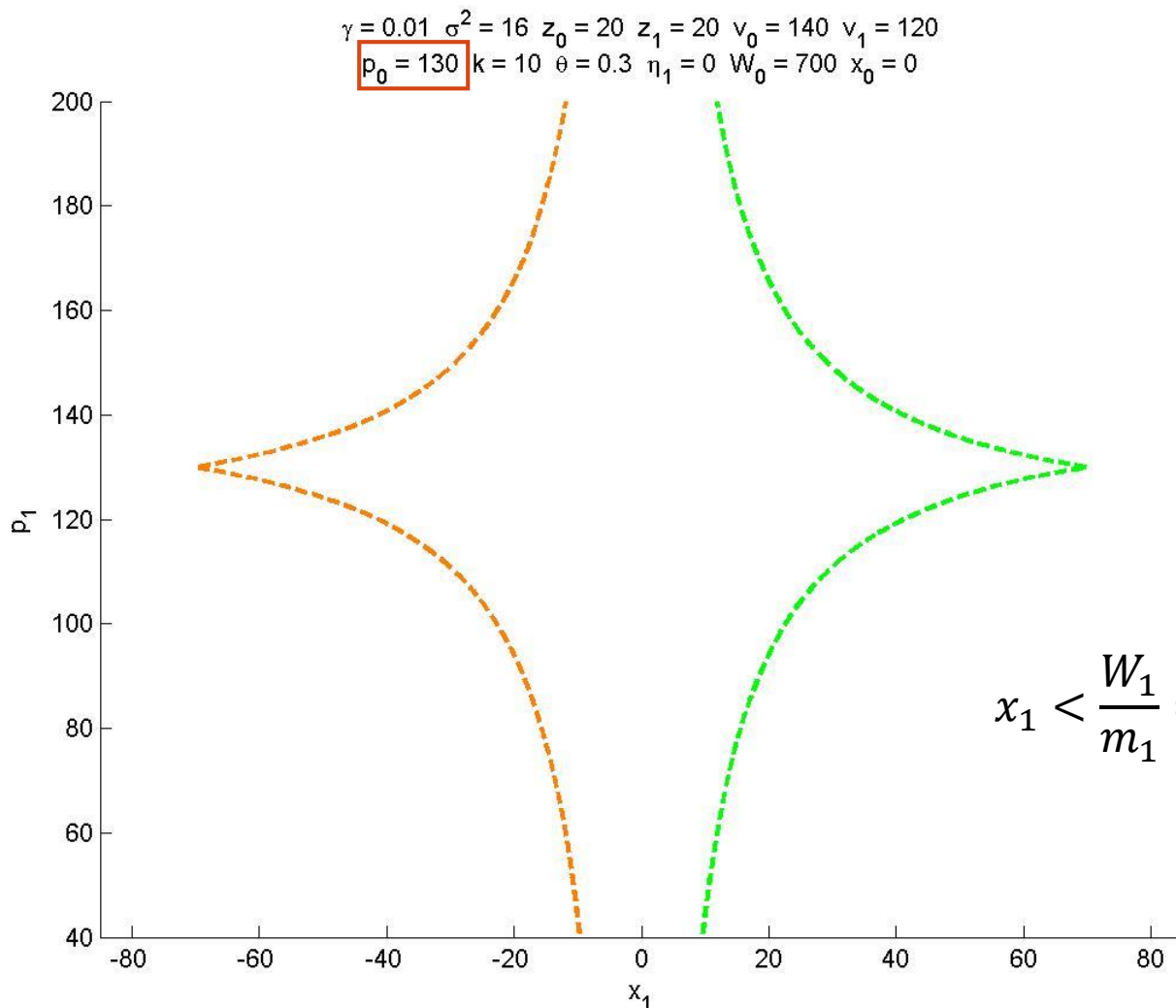
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$$\sigma_{t+1} = \sigma + \theta |\Delta v_t|$$

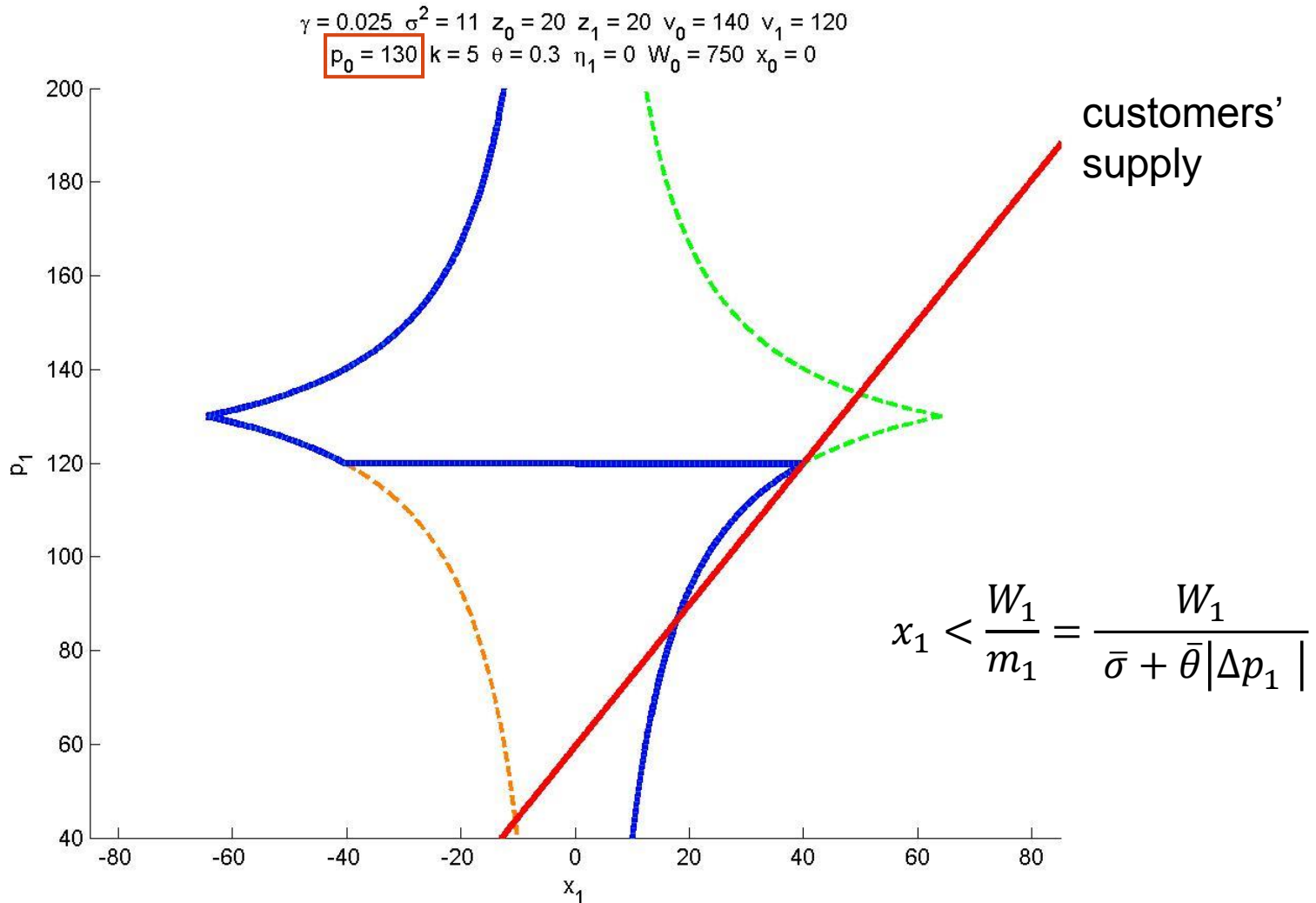
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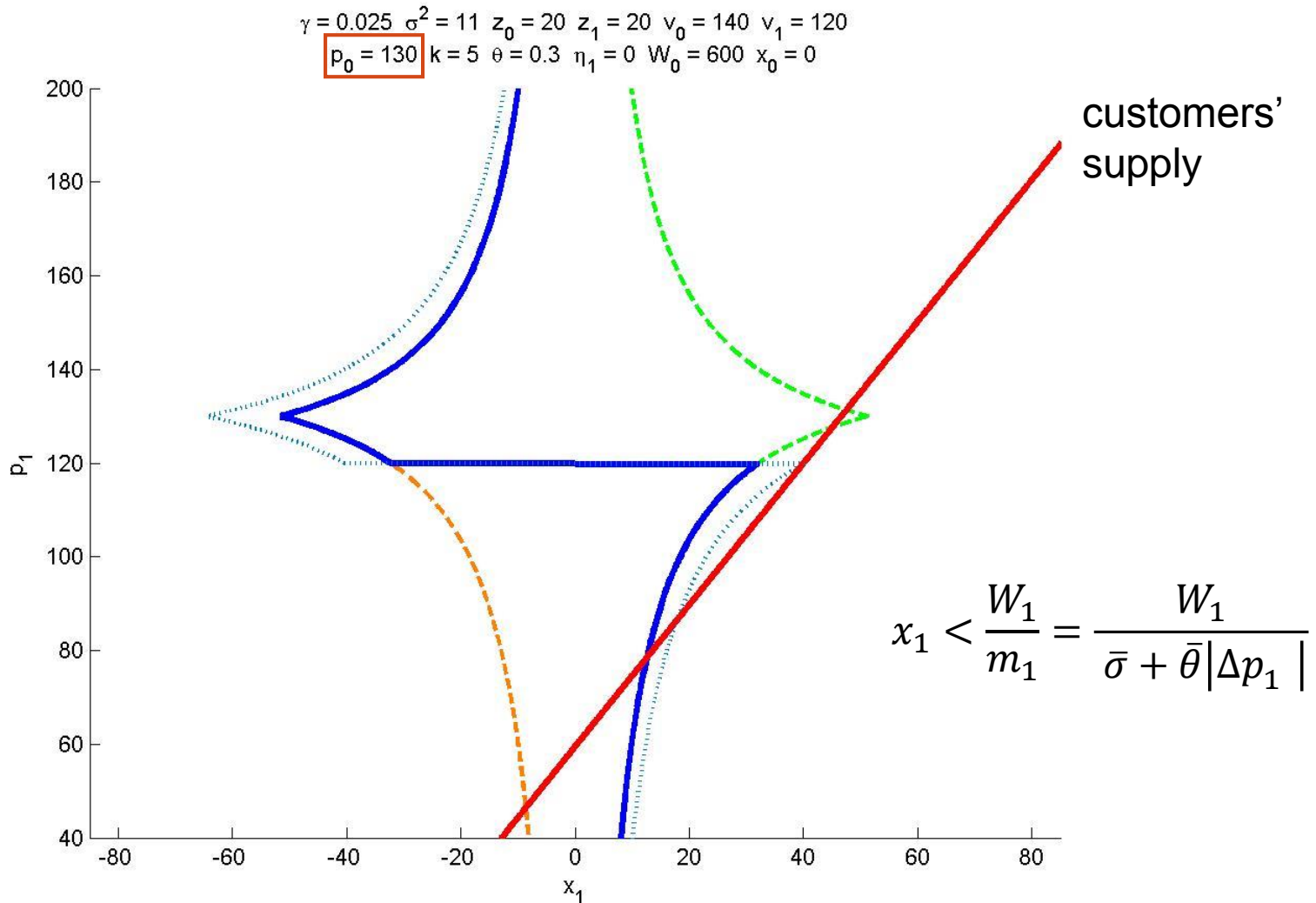
1. Margin Spiral – Increased Volatility



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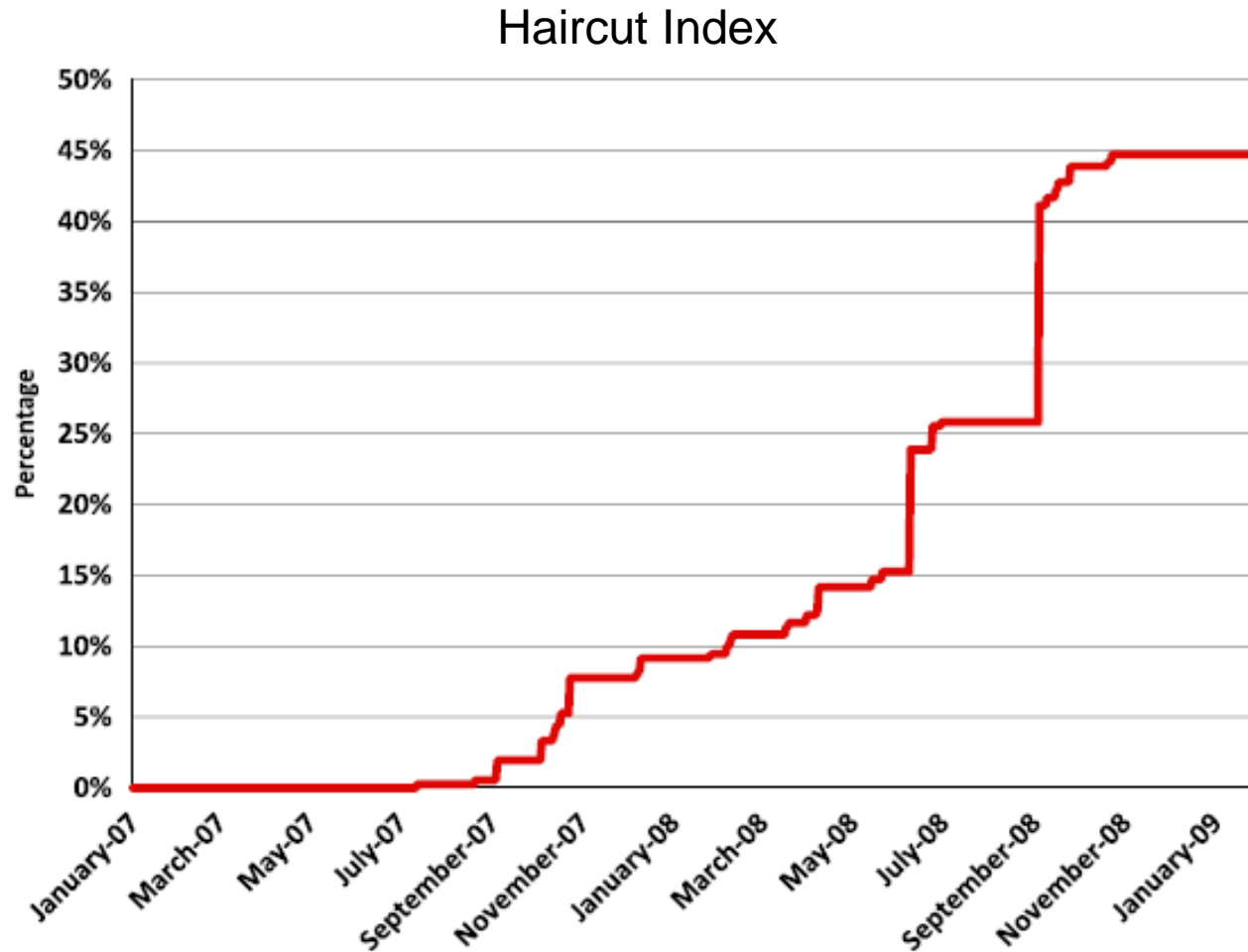


1. Margin Spiral – Increased Volatility





Data Gorton and Metrick (2011)



“The Run on Repo”

Copeland, Martin, Walker (2011)

Margins **stable** in tri-party repo market

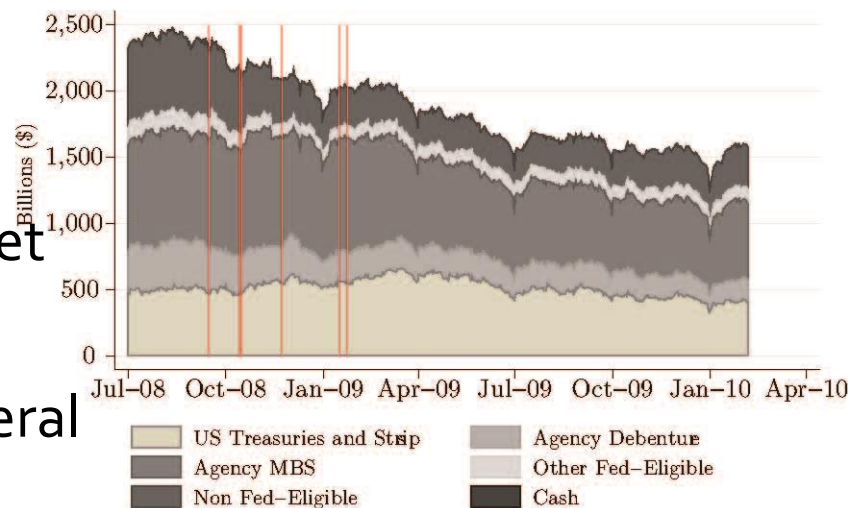
- contrasts Gorton and Metrick
- no general run on certain collateral

Run (non-renewed financing) only on select **counterparties**

- Bear Stearns (anecdotally)
- Lehman (in the data)

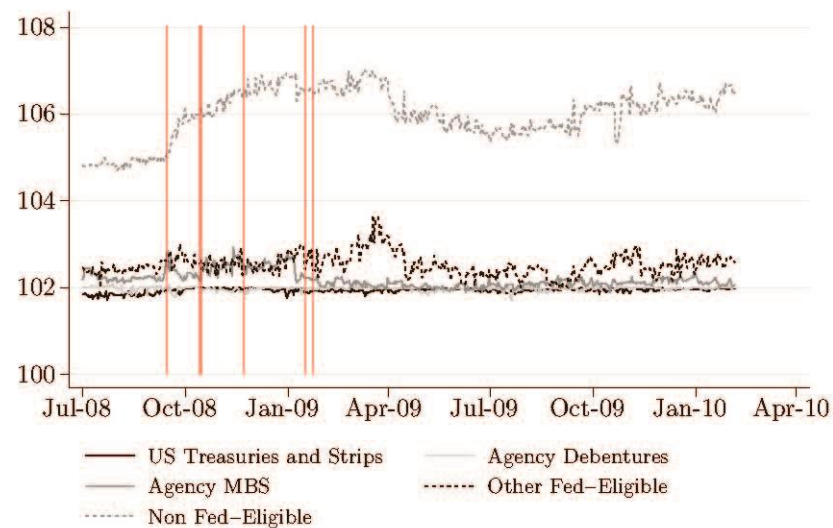
Like 100% haircut...
(**counterparty specific!**)

Figure 6: Stacked Graph of Collateral



Note: July 17, 2008 excluded because no data was available for BNYM on that date. Red lines correspond to important market events. From left to right: 9/15/08 (Lehman), 10/14/08 (9 banks receive aid), 10/16/08 (UBS), 11/23/08 (Citi), 1/16/09 (B of A), 1/24/09 (Citi).

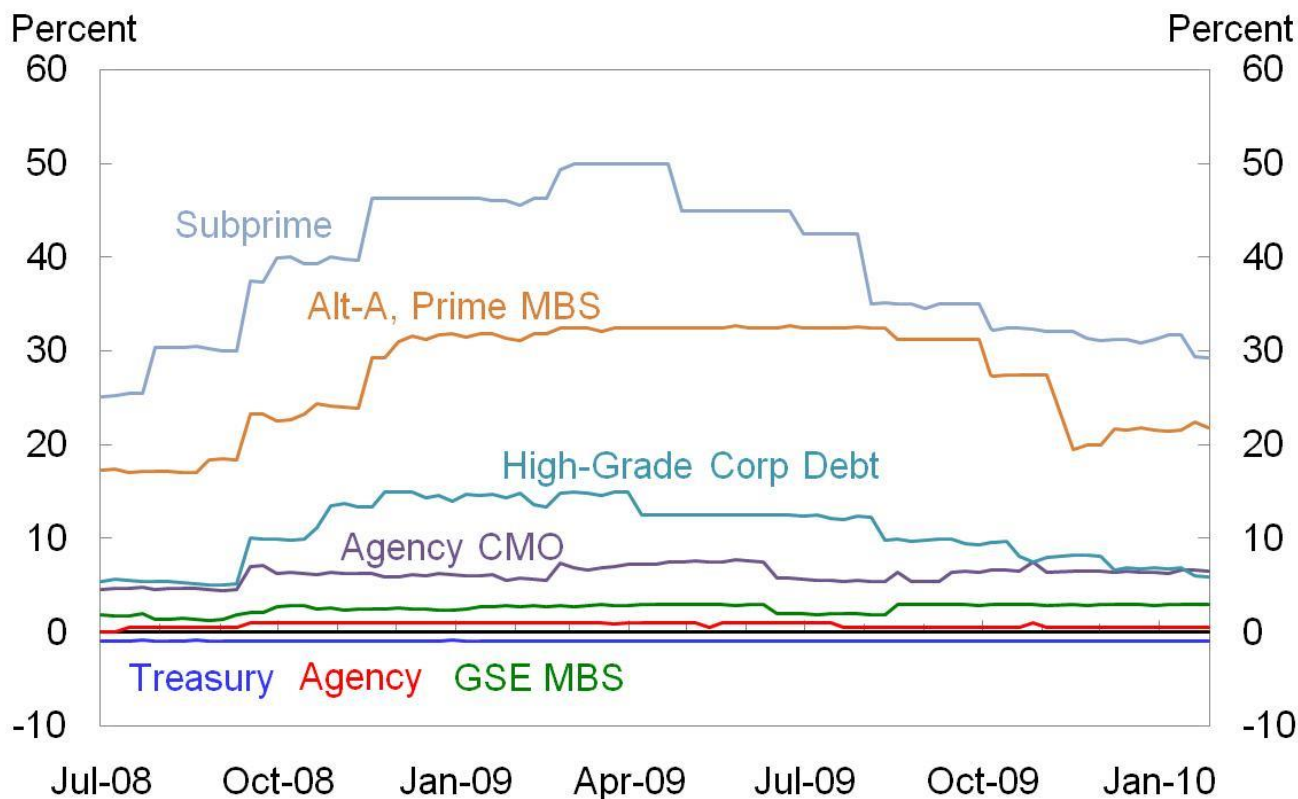
Figure 7: Median Haircuts by Asset Type



Note: Red lines correspond to important market events. From left to right: 9/15/08 (Lehman), 10/14/08 (9 banks receive aid), 10/16/08 (UBS), 11/23/08 (Citi), 1/16/09 (B of A), 1/24/09 (Citi).

Bilateral and Tri-party Haircuts?

Differences in Median Haircuts



Source: FRBNY Calculations

BP: Multiple Assets

- Dealer maximizes expected profit per capital use
 - Expected profit $E_1[v^j] - p^j = \Lambda^j$
 - Capital use m^j
- Dealers
 - Invest only in securities with highest ratio Λ^j/m^j
- Hence, illiquidity/margin ratio Λ^j/m^j is constant

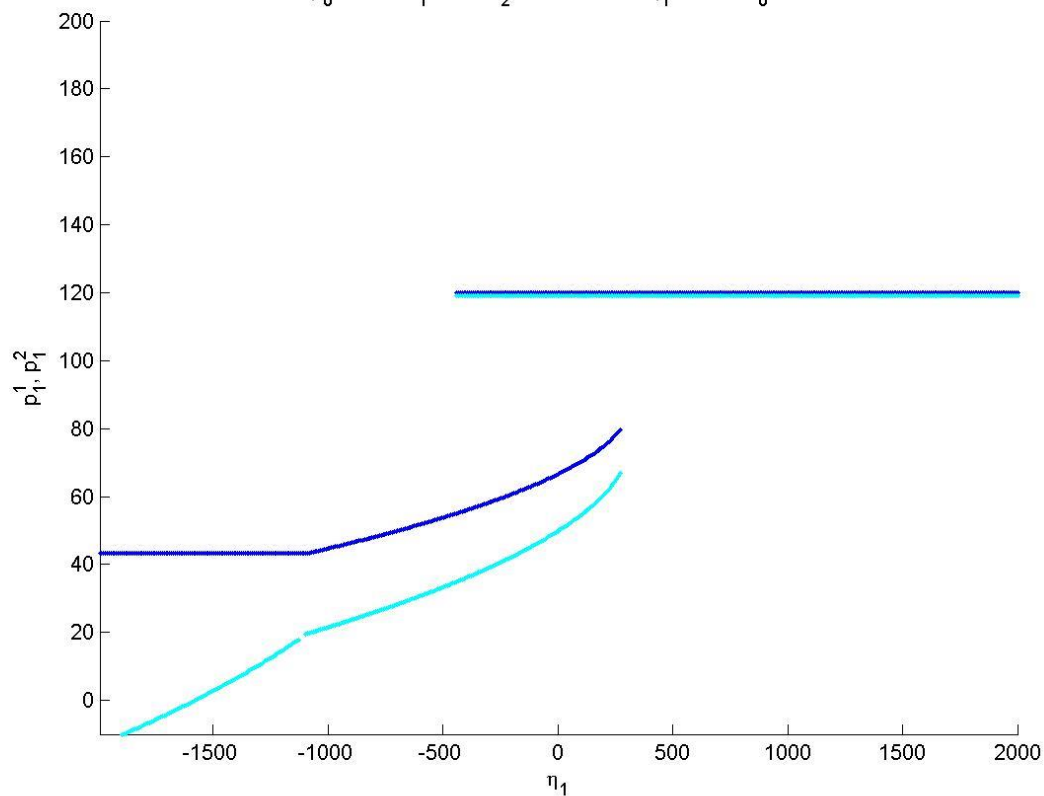
BP: Commonality & Flight to Quality

- Commonality
 - Since funding liquidity is driving common factor
- Flight to Quality
 - Quality=Liquidity
Assets with lower fund vol. have better liquidity
 - Flight
liquidity differential widens when funding liquidity becomes tight

BP: Flight to Quality

$m^2 = \text{Volatility of Security 2} = 2 > 1 = \text{Volatility of Security 1} = m^1$

$\gamma = 0.015 \quad z_0 = 20 \quad z_1 = 20 \quad v_0 = 140 \quad v_1 = 120$
 $p_0 = 130 \quad \sigma_1 = 10 \quad \sigma_2 = 15 \quad \theta = 0.3 \quad \eta_1 = 2000 \quad x_0 = 0$



Macro-literature on Frictions

1. Net worth effects:

- a. Persistence: Carlstrom & Fuerst
- b. Amplification: Bernanke, Gertler & Gilchrist
"Kocherlakota critique"

2. Volatility effects: impact credit quantity constraints

- a. Instability: Brunnermeier & Sannikov
- b. Margin spirals : Brunnermeier & Pederson
- c. Endogenous constraints: Geanakoplos

3. Demand for liquid assets & Bubbles – "self insurance"

- a. OLG, Aiyagari, Bewley, Krusell-Smith, Holmstrom-Tirole,...

4. Financial intermediaries & Theory of Money